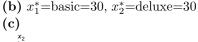
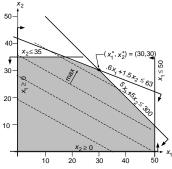
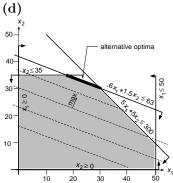
Full Download: http://downloadlink.grg/product/solutions-manual-for-optimization-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operation-in

**2-1.** (a) max  $200x_1 + 350x_2$  (max total profit), s.t.  $5x_1 + 5x_2 \le 300$  (legs),  $0.6x_1 + 1.5x_2 \le 63$  (assembly hours),  $x_1 \le 50$  (wood tops),  $x_2 \le 35$  (glass tops),  $x_1 \ge 0$ ,  $x_2 \ge 0$  (b)  $x_1^* = \text{basic} = 30$ ,  $x_2^* = \text{deluye} = 30$ 

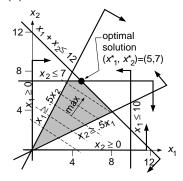


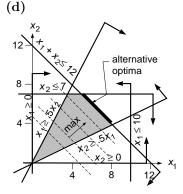




All optimal from  $\mathbf{x} = (30, 30)$  to  $\mathbf{x} = (17.5, 35)$ .

**2-2.** (a) max  $.11x_1 + .17x_2$  (max total return), s.t.  $x_1 + x_2 \le 12$  (\$12 million investment),  $x_1 \le 10$  (max \$10 million domestic),  $x_2 \le 7$  (max \$7 million foreign),  $x_1 \ge .5x_2$  (domestic at least half foreign),  $x_2 \ge .5x_1$  (foreign at least half domestic),  $x_1 \ge 0$ ,  $x_2 \ge 0$  (b)  $x_1^*$ =domestic=\$5 million,  $x_2^*$ = foreign=\$7 million



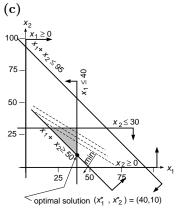


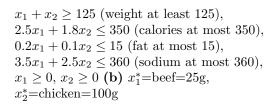
All optimal from  $\mathbf{x} = (5,7)$  to  $\mathbf{x} = (8,4)$ .

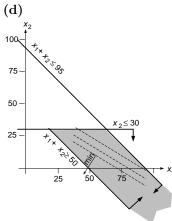
**2-3.** (a) min  $3x_1 + 5x_2$  (min total cost), s.t.  $x_1 + x_2 \ge 50$  (at least 50 thousand acres),  $x_1 \le 40$  (at most 40 thousand from Squawking Eagle),  $x_2 \le 30$  (at most 30 thousand from Crooked Creek),  $x_1 \ge 0$ ,  $x_2 \ge 0$  (b)  $x_1^*$ =Squawking Eagle=40 thousand,  $x_2^*$ =Crooked Creek=10 thousand

 $<sup>^1{\</sup>rm Supplement}$  to the 2nd edition of Optimization~in~Operations~Research, by Ronald L. Rardin, Pearson Higher Education, Hoboken NJ, ©2017.

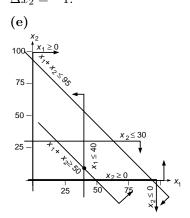
<sup>&</sup>lt;sup>2</sup>As of September 24, 2015





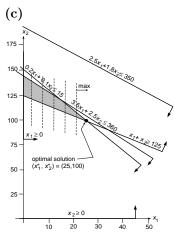


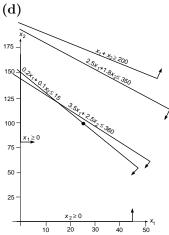
Improves forever in direction  $\Delta x_1 = 1$ ,  $\Delta x_2 = -1$ .



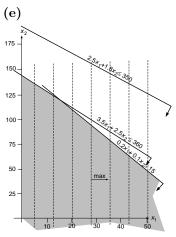
 $x_2 = 0$  leaves no feasible.

**2-4**. (a) max  $x_1$  (max beef content), s.t.

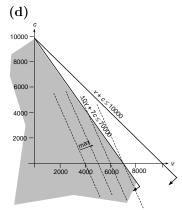




 $x_1 + x_2 \ge 200$  leaves no feasible.

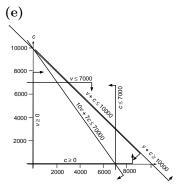


Improve forever in direction  $\Delta x_1 = 1$ ,  $\Delta x_2 = -2$ .

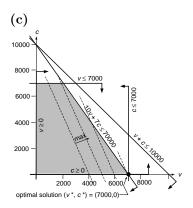


Improves forever in direction  $\Delta v = 10$ ,  $\Delta c = -7$ .

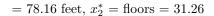
**2-5**. **(a)** max 450v + 200c (max total profit), s.t.  $10v + 7c \le 70000$  (water at most 70000 units),  $v + c \le 10000$  (total acreage 10000),  $v \le 7000$  (at most 70% vegetables),  $c \le 7000$  (at most 70% cotton),  $v \ge 0$ ,  $c \ge 0$  **(b)**  $v^* = 7000$ ,  $c^* = 0$ 

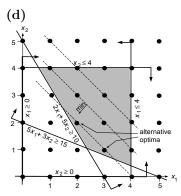


No solution with v + c = 10000.



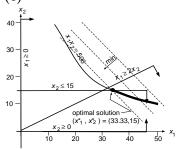
**2-6.** (a) min  $x_1 + x_2$  (min used stock), s.t.  $5x_1 + 3x_2 \ge 15$  (cut at least 15 long rolls),  $2x_1 + 5x_2 \ge 10$  (cut at least 10 short rolls),  $x_1 \le 4$  (at most 4 times on pattern 1),  $x_2 \le 4$  (at most 4 times on pattern 2),  $x_1, x_2 \ge 0$  and integer. (b) Partial cuts make no physical sense because all unused material is scrap. (c) Either  $x_1^* = x_2^* = 2$ , or  $x_1^* = 3$ ,  $x_2^* = 1$ 

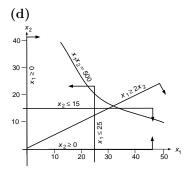




(e) Both (2,2) and (3,1) are feasible and lie on the best contour of the objective.

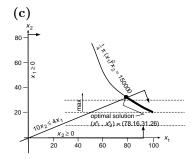
**2-7**. (a) min  $16x_1 + 16x_2$  (min total wall area), s.t.  $x_1x_2 = 500$  (500 sqft pool),  $x_1 \ge 2x_2$  (length at least twice width),  $x_2 \le 15$  (width at most 15 ft),  $x_1 \ge 0$ ,  $x_2 \ge 0$  (b)  $x_1^* = \text{length} = 33\frac{1}{3}$  feet,  $x_2^* = \text{width} = 15$  feet (c)

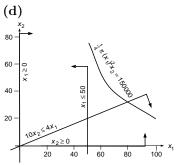




 $x_1 \leq 25$  leaves no feasible.

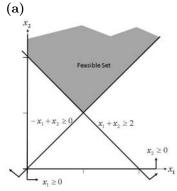
**2-8.** (a) max  $x_2$  (max number of floors), s.t.  $\pi/4(x_1)^2x_2 = 150000$  (150000 sqft floor space),  $10x_2 \le 4x_1$  (height at most 4 times diameter),  $x_1 \ge 0$ ,  $x_2 \ge 0$  (b)  $x_1^*$  = diameter





 $x_1 \leq 50$  leaves no feasible.

**2-9**.



(b) min  $x_2$  (c) min  $x_1 + x_2$  (d) max  $x_2$  (e)  $x_2 \le 1/2$ 

**2-10**.

```
(a)
x_{2}
Feasible Set
2x_{1} + 3x_{2} \ge 6
x_{1} \ge 0
```

```
(b) min x_1 + x_2 (c) min x_1 (d) max x_1 (e)
x_1 + x_2 \le 1
2-11. (a) min \sum_{i=3}^{4} i \sum_{j=1}^{2} y_{i,j}
(b) \max \sum_{i=1}^{4} \overline{iy_{i,3}}

(c) \max \sum_{i=1}^{p} \alpha_{i} y_{i,4}

(d) \min \sum_{i=1}^{4} \delta_{i} y_{i}
(e) \sum_{j=1}^{4} y_{i,j} = s_i, i = 1, ..., 3

(f) \sum_{j=1}^{4} a_{j,i} y_j = c_i, i = 1, ..., 3
2-12. (a)
\sum_{i=1}^{17} x_{i,j,t} \le 200, \ j = 1, \dots, 5; t = \dots, 7; 35
constraints
(b) \sum_{i=1}^{5} \sum_{t=1}^{7} x_{5,j,t} \le 4000; 1 constraint
\sum_{j=1}^{5} x_{i,j,t} \ge 100, \ i = 1, \dots, 17; t = 1, \dots, 7;
119 constraints
2-13.
            model; param m; param n; param
p; set products := 1 .. m; set lines
:= 1 .. n; set weeks := 1 .. p; var
x{i in products, j in lines, t in
weeks >= 0; subject to
# part (a)
linecap {j in lines, t in weeks}: sum
{i in products} x[i,j,t] \le 200;
# part (b)
prod5lim: sum {j in lines, t in
weeks \{x[5,j,t] \le 4000;
# part (c)
minprodn{i in products, t in weeks}:
sum \{j \text{ in lines}\}\ x[i,j,t] >= 100;
```

data; param m := 17; param n := 5;

param p := 7;

```
2-14. (a)
\sum_{j=1}^{9} x_{i,j,t} \le p_i, \ i = 1, \dots, 47; t = 1, \dots, 10;
470 constraints
(b) 0.25 \sum_{i=1}^{47} \sum_{j=1}^{9} x_{i,j,t} \leq \sum_{i=1}^{47} x_{i,4,t}; t =
1, \ldots, 5; 5 constraints
(c) x_{i,1,t} \geq x_{i,i,t} \ i = 1, \dots, 47; \ j =
1, \ldots, 9; \ t = 1, \ldots, 10; 4230  constraints
        model; param m; param n; param
q; set plots := 1 .. m; set crops :=
1 .. n; set years := 1 .. q; param p
{i in plots }; var x{i in plots, j
crops, t in years} >= 0; subject to
# part (a)
acrelims {i in plots, t in years }:
sum {j \text{ in crops }} x[i,j,t] \leftarrow p[i];
# part (b)
crop4min {t in years: t <= 5 }:</pre>
0.25* sum {i in plots, j in crops }
x[i,j,t] \le sum \{i \text{ in plots }\}
x[i,4,t];
# part (c)
beam1st {i in plots, j in crops, t in
years\{\}: x[i,1,t] >= x[i,j,t];
data; param m := 47; param n := 9;
param q := 10;
2-16. (a) f(y_1, y_2, y_3) \stackrel{\Delta}{=} (y_1)^2 y_2/y_3,
g_1(y_1, y_2, y_3) \stackrel{\Delta}{=} y_1 + y_2 + y_3, b_1 = 13,
g_2(y_1, y_2, y_3) \stackrel{\Delta}{=} 2y_1 - y_2 + 9y_3, b_2 = 0,
g_3(y_1, y_2, y_3) \stackrel{\Delta}{=} y_1, b_3 = 0, g_4(y_1, y_2, y_3) \stackrel{\Delta}{=} y_3,
(b) f(y_1, y_2, y_3) \stackrel{\Delta}{=} 13y_1 + 22y_2 + 10y_2y_3 + 100,
g_1(y_1, y_2, y_3) \stackrel{\Delta}{=} y_1 - y_2 + 9y_3, b_1 = -5,
g_2(y_1, y_2, y_3) \stackrel{\Delta}{=} 8y_2 - 4y_3, b_2 = 0, g_3(y_1, y_2, y_3)
\stackrel{\Delta}{=} y_1, b_3 = 0, g_4(y_1, y_2, y_3) \stackrel{\Delta}{=} y_2, b_4 = 0,
g_5(y_1, y_2, y_3 \stackrel{\Delta}{=} y_3, b_5 = 0,
2-17. (a) Linear because LHS is a weighted
sum of the decision variables. (b) Linear
because both LHS and RHS are weighted
sums of the decision variables. (c) Nonlinear
because LHS has reciprocal 1/x_9. (d) Linear
because LHS is a weighted sum of the decision
variables. (e) Nonlinear because LHS has
(x_i)^2 terms. (f) Nonlinear because LHS has
\log(x_1) term, and RHS has a product of
```

variables. (g) Nonlinear because LHS has max operator. (h) Linear because LHS is a weighted sum of the decision variables.

**2-18.** (a) LP because the objective and all constraints are linear. (b) NLP because of the nonlinear objective function with reciprocal of  $w_2$ . (c) NLP because of the nonlinear first constraint. (d) LP because the objective and all constraints are linear.

**2-19.** (a) Continuous because fractions make sense. (b) Discrete because they either closed or not. (c) Discrete because a specific process must be used. (d) Continuous because fractions can probably be ignored.

**2-20.** (a)  $\sum_{j=1}^{8} x_j = 3$  (b)  $x_1 + x_2 + x_4 + x_5 \ge 2$  (c)  $x_3 + x_8 \le 1$  (d)  $x_4 \ge x_1$ 

**2-21.** (a) max  $85x_1 + 70x_2 + 62x_3 + 93x_4$  (max total score), s.t.

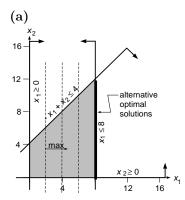
 $700x_1 + 400x_2 + 300x_3 + 600x_4 \le 1000$  (\$1 million available),  $x_j = 0$  or 1, j = 1, ..., 4 (b) Fund 2 and 4, i.e.  $x_1^* = x_3^* = 0$ ,  $x_2^* = x_4^* = 1$ 

**2-22.** (a) min  $43y_1 + 175y_2 + 60y_3 + 35y_4$  (min total land cost), s.t.  $y_2 + y_4 \ge 1$  (service NW),  $y_1 + y_2 + y_4 \ge 1$  (service SW),  $y_2 + y_3 \ge 1$  (service capital),  $y_1 + y_4 \ge 1$  (service NE),  $y_1 + y_2 + y_3 \ge 1$  (service SE),  $y_j = 0$  or  $1, j = 1, \dots, 4$  (b) Build 3 and 4, i.e.  $y_1^* = y_2^* = 0, y_3^* = y_4^* = 1$ 

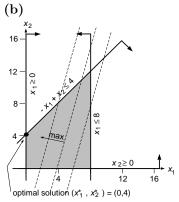
**2-23**. (a) ILP because the objective and all constraints are linear, but variables are discrete. (b) NLP because the objective is nonlinear and all variables are continuous. (c) INLP because the objective is nonlinear and variables are discrete. (d) LP because the objective and all constraints are linear, and all variables are continuous. (e) INLP because the one constraint is nonlinear, and  $z_3$  are discrete. (f) ILP because the objective and all constraints are linear, but variables  $z_1$  and  $z_3$  are discrete. (g) LP because the objective and all constraints are linear, and all variables are continuous. (h) INLP because the objective is nonlinear and  $z_3$  is discrete.

2-24. (a) Model (d) because LP's are generally more tractable than ILP's. (b) Model (d) because LP's are generally more tractable than NLP's. (c) Model (d) because LP's are generally more tractable than INLP's. (d) Model (f) because ILP's are generally more tractable than INLP's. (e) Model (g) because LP's are generally more tractable than ILP's.

2-25.

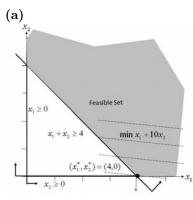


Alternative optima from  $x_1^* = 8$ ,  $x_2^* = 0$  to  $x_1^* = 8$ ,  $x_2^* = 12$ 

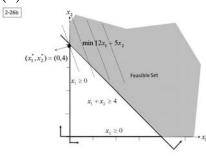


Unique optimum  $x_1^* = 0$ ,  $x_2^* = 4$  (c) Helping one can hurt the other.

2-26.



Unique optimum  $x_1^* = 4, x_2^* = 0$ (b)



Unique optimum  $x_1^* = 0$ ,  $x_2^* = 4$  (c) Helping one can hurt the other.

**2-27**. (a) min

 $.092x_4 + .112x_5 + .141x_6 + .420x_9 + .719x_{12}$ (min total cost),

s.t.  $x_4 + x_5 + x_6 + x_9 + x_{12} = 16000 (16000 \text{m})$ line),

 $.279x_4 + .160x_5 + .120x_6 + .065x_9 + .039x_{12} \le$ 1600 (at most 1600 Ohms resistance),

 $.00175x_4 + .00130x_5 + .00161x_6 + .00095x_9 +$  $.00048x_{12} \le 8.5$  (at most 8.5 dBell attenuation),

 $x_4, x_5, x_6, x_9, x_{12} \ge 0$ 

**(b)** Nonzeros:  $x_5^* = 1000, x_{12}^* = 15000$ 

**2-28**. (a) Pump rates are the decisions to be made.

**(b)**  $u_j \stackrel{\triangle}{=}$  the capacity of pump  $j, c_j \stackrel{\triangle}{=}$  the pumping cost of pump j(c) min  $\sum_{j=1}^{10} c_j x_j$ (d)  $x_1 + x_4 + x_7 \le 3000$  (well 1),

 $x_2 + x_5 + x_8 \le 2500 \text{ (well 2)},$  $x_3 + x_6 + x_9 + x_{10} \le 7000 \text{ (well 3)}$ 

(e)  $x_j \le u_j, j = 1, ..., 10$ (f)  $\sum_{j=1}^{10} x_j \ge 10000$ 

(g)  $x_j \ge 0, j = 1, \dots, 10$ 

(h) A single objective LP because the one objective and all constraints are linear, and all variables are continuous.

(i)  $x_1^* = x_2^* = x_3^* = 1100, x_4^* = x_6^* = 1500,$  $x_5^* = 1400, x_7^* = 400; x_8^* = x_{10}^* = 0, x_9^* = 1900$ 

**2-29**. (a) The decisions to be made are which projects to undertake.

(b)  $p_j \triangleq$  the profit for project  $j, m_j \triangleq$  the man-days required on project j, and  $t_i \stackrel{\Delta}{=}$  the CPU time required on project j.

(c)  $\max \sum_{j=1}^{8} p_j x_j$ (d)  $7 \le \left(\sum_{j=1}^{8} m_j x_j\right) / 240 \le 10$ 

(e)  $\sum_{j=1}^{8} t_j x_j \le 1000$  (computer time),  $\sum_{j=1}^{8} x_j \geq 3$  (select at least 3);  $x_3 + x_4 + x_5 + x_8 \ge 1$  (include at least 1 of director's favorites)

(f)  $x_j = 0$  or  $1, j = 1, \dots, 8$ 

(g) A single objective ILP because the one objective and all constraints are linear, but variables are discrete.

(h)  $x_1^* = x_3^* = x_6^* = x_7^* = 1$ , others = 0

2-30. (a) We must decide what quantities to move from surplus sites to fulfill each need.

(b)  $s_i \stackrel{\Delta}{=}$  the supply available at  $i, r_j \stackrel{\Delta}{=}$  the quantity needed at j,  $d_{i,j} \triangleq$  the distance from i to j.

(c)  $\min_{z} \sum_{i=1}^{4} \sum_{j=1}^{7} d_{i,j} x_{i,j}$ 

(d)  $\sum_{j=1}^{7} x_{i,j} = s_i, i = 1, ..., 4$ (e)  $\sum_{i=1}^{4} x_{i,j} = r_j, j = 1, ..., 7$ (f)  $x_{i,j} \ge 0, i = 1, ..., 4, j = 1, ..., 7$ 

(g) A single objective LP because the one objective and all constraints are linear, and all variables are continuous.

**(h)** Nonzeros:  $x_{1,1}^* = 81, x_{1,2}^* = 93,$  $x_{1,3}^* = 166, x_{1,5}^* = 90, x_{1,6}^* = 85, x_{1,7}^* = 145,$   $x_{2,2}^* = 301, x_{3,1}^* = 166, x_{3,4}^* = 105, x_{4,3}^* = 99$ 

**2-31**. (a) The values to be chosen are the

coefficients in the estimating relationship.

- **(b)** min  $\sum_{j=1}^{n} (c_j k/(1 + e^{a+bf_j}))^2$  (min total squared error)
- (c) Single objective NLP because the objective is quadratic, there are no constraints, and all variables are continuous.
- **2-32**. **(a)** The decisions to be made are where to assign each teacher.
- **(b)** min  $\sum_{i=1}^{22} \sum_{j=1}^{22} c_{i,j} x_{i,j}$  (min total cost),  $\max \sum_{i=1}^{22} \sum_{j=1}^{22} t_{i,j} x_{i,j} \text{ (max total teacher)}$ preference), max  $\sum_{i=1}^{22} \sum_{j=1}^{22} s_{i,j} x_{i,j}$  (max total supervisor preference), max  $\sum_{i=1}^{22} \sum_{j=1}^{22} p_{i,j} x_{i,j}$  (max total principal preference)
- (c)  $\sum_{j=1}^{22} x_{i,j} = 1, i = 1, \dots, 22$  (each teacher
- (d)  $\sum_{i=1}^{22} x_{i,j} = 1, j = 1, \dots, 22$  (each school
- (e)  $x_{i,j} = 0$  or  $1, i, j = 1, \dots, 22$
- (f) A multiobjective ILP because the 4 objectives and all constraints are linear, but variables are discrete.
- **2-33**. (a) Each task must go to Assistant 0 or Assistant 1.
- **(b)** max  $100(1-x_1) + 80x_1 + 85(1-x_2) +$  $70x_2 + 40(1-x_3) + 90x_3 + 45(1-x_4) +$  $85x_4 + 70(1-x_5) + 80x_5 + 82(1-x_6) + 65x_6$
- (c)  $\sum_{j=1}^{6} x_j = 3$
- (d)  $x_5 = x_6$
- (e)  $x_j = 0$  or  $1, j = 1, \dots, 6$
- (f) A single objective ILP because the one objective and all constraints are linear, but variables are discrete.
- (g)  $x_2^* = x_3^* = x_4^* = 1$ , others = 0
- 2-34. (a) Batch sizes are the decisions to be
- **(b)** min  $x_j/d_j$ , j = 1, ..., 4 (each burger j)
- (c)  $\sum_{j=1}^{4} t_j d_j / x_j \le 60$
- (d)  $0 \le x_j \le u_j, j = 1, \dots, 4$
- (e) Multiobjective NLP because the first constraint is nonlinear and all variables are continuous.
- **2-35**. (a) The issue is how many cars to move from where to where.

- (b) Relatively large values can be rounded if fractional without much loss, and continuous is more tractable.
- (c)  $c_{i,j} \stackrel{\Delta}{=}$  the cost of moving a car from i to j,  $p_i \stackrel{\Delta}{=}$  the number of cars presently at  $j, n_i \stackrel{\Delta}{=}$ the number of cars required at j
- (d) min  $\sum_{i=1}^{5} \sum_{j=1, j \neq i}^{5} c_{i,j} x_{i,j}$
- (e)  $\sum_{i=1, i \neq k}^{5} x_{i,k} \sum_{j=1, j \neq k}^{5} x_{k,j} = n_k p_k,$   $k = 1, \dots, 5$  (each region k)
- (f)  $x_{i,j} \geq 0, i, j = 1, \dots, 5, i \neq j$
- (g) A single objective LP because the one objective and all constraints are linear, and all variables are continuous.
- (h) Nonzero values:  $x_{4,2}^* = 115, x_{4,3}^* = 165,$  $x_{5.1}^* = 85, x_{5.3}^* = 225$
- 2-36. (a) We must decide how much of what fuel to burn at each plant.

- (b)  $\min \sum_{f=1}^{4} \sum_{p=1}^{23} c_{f,p} x_{f,p}$ (c)  $\min \sum_{f=1}^{4} s_f \sum_{p=1}^{23} x_{f,p}$ (d)  $\sum_{f=1}^{4} e_f x_{f,p} \ge r_p, \ p = 1, \dots, 23$  (each plant p); 23 constraints
- (e)  $x_{f,p} \ge 0, f = 1, \dots, 4, p = 1, \dots, 23; 92$ constraints
- (f) A multiobjective LP because the 2 objectives and all constraints are linear, and all variables are continuous.
- **2-37**. (a) The available options are to buy whole logs or green lumber.
- (b) Relatively large magnitudes can be rounded without much loss, and continuous is more tractable.
- (c) min
- $70x_{10} + 200x_{15} + 620x_{20} + 1.55y_1 + 1.30y_2$
- (d)  $100(.09)x_{10} + 240(.09)x_{15} + 400(.09)x_{20} +$  $.10y_1 + .08y_2 \ge 2350$
- (e)  $x_{10} + x_{15} + x_{20} \le 1500$  (sawing capacity),  $100x_{10} + 240x_{15} + 400x_{20} + y_1 + y_2 \le 26500$ (drying capacity)
- (f)  $x_{10} \leq 50$  (size 10 log availability),  $x_{15} \leq 25$  (size 15 log availability),  $x_{20} \leq 10$ (size 20 log availability),  $y_1 \leq 5000$  (grade 1 green lumber availability)
- (g)  $x_{10}, x_{15}, x_{20}, y_1, y_2 \ge 0$
- (h) A single objective LP because the one

objective and all constraints are linear, and all variables are continuous.

(i) 
$$x_{10}^* = 50$$
,  $x_{15}^* = 25$ ,  $x_{20}^* = 5$ ,  $y_1^* = 5000$ ,  $y_2^* = 8500$ 

**2-38**. (a) Decisions to be made are when to schedule each film.

(b) min 
$$\sum_{j=1}^{m-1} \sum_{j'=j+1}^{n} a_{j,j'} \sum_{t=1}^{n} x_{j,t} x_{j',t}$$
  
(c)  $\sum_{t=1}^{n} x_{j,t} = 1$ ,  $j = 1, \ldots, m$  (each film  $j$ )  
(d)  $\sum_{j=1}^{m} x_{j,t} \le 4$ ,  $t = 1, \ldots, n$  (each time  $t$ )  
(e)  $x_{j,t} = 0$  or  $1, j = 1, \ldots, m; t = 1, \ldots, n$   
(f) A single objective INLP because the one objective is nonlinear, and variables are discrete. (g) model; param  $m$ ; param  $n$ ;

objective is nonlinear, and variables are discrete. (g) model; param m; param n; set films := 1 .. m; set slots := 1 .. n; var x{j in films, t in slots } binary; param a{ j in films, jp in films }; minimize totconflict: sum{ j in films, jp in films: j < m and jp > j } a[j,jp]\*sum {t in slots} x[j,t]\*x[jp,t]; subject to allin {j in films $\}$ : sum $\{$  t in slots $\}$  x[j,t] = 1;

max4 {t in slots}:sum{j in films} x[j,t] <= 4;**2-39**. (a) We need to decide both which

offices to open and how to service customers from them.

(b) Offices must either be opened or not.

(c)  $f_i \triangleq \text{fixed cost of site } i, c_{i,j} \triangleq \text{unit cost of }$ audits at j from i,  $r_i \stackrel{\Delta}{=}$  required number of audits in state j

(d) 
$$\min \sum_{i=1}^{5} \sum_{j=1}^{5} c_{i,j} r_j x_{i,j} + \sum_{i=1}^{5} f_i y_i$$

(e)  $\sum_{i=1}^{5} x_{i,j} = 1, j = 1, ..., 5$  (each location

(f)  $x_{i,j} \le y_i, i, j = 1, ..., 5$  (each site i, location j combination)

(g) 
$$x_{i,j} \ge 0$$
,  $i, j = 1, ..., 5$ ,  $y_i = 0$  or 1,  $i = 1, ..., 5$ 

(h) A single objective ILP because the one objective and all constraints are linear, but the  $y_i$  variables are discrete.

(i) Nonzeros:

$$x_{2,2}^* = x_{2,4}^* = x_{3,1}^* = x_{3,3}^* = x_{5,5}^* = 1,$$
  $y_2^* = y_3^* = y_5^* = 1$  (j) model; param m; param n; set sites := 1 .. m; set

states := 1 .. n; var x{i in sites, j in states } >= 0; var y{i in sites } binary; param c {i in sites, j in states }; param f { i in sites } binary; param r { j in states }; minimize totcost: sum{i in sites, j in states  $c[i,j]*r[j]*x[i,j] + sum{i}$ in sitesf[i]\*y[i]; x[j,t]\*x[jp,t];subject to doeach{j in states}: sum{i in sitesx[i,j] = 1; switch {i in sites, j in states  $\}$ :  $x[i,j] \le y[i]$ ; data; param m := 5; param n := 5; param f := 1 160 2 49 3 246 4 86 4 100; param r := 1 200 2 100 3 300 4100 5 200; param c: 1 2 3 4 5 := 1 0.0 0.4 0.8 0.4 0.8 2 0.7 0.0 0.8 0.4 0.4 3 0.6 0.4 0.0 0.5 0.4 4 0.6 0.4 0.9 0.0 0.4 5 0.9 0.4 0.7 0.4 0.0 ; **2-40**. (a)  $\max \sum_{j=1}^{8} r_j x_j$ , subject to,  $\sum_{j=1}^{8} x_j \le 4, \ x_1 + x_2 + x_3 \ge 2,$  $x_4 + x_5 + x_6 + x_7 + x_8 \ge 1$ ,  $x_2 + x_3 + x_4 + x_8 \ge 2, x_1 \dots x_8 = 0 \text{ or } 1 \text{ (b)}$ model; param n ; set games := 1 .. n; #ratings param r{j in games}; #home? param h{j in games}; #state? param s{j in games}; #cover? var x{j in in games } r[j] \*x[j]; subject to capacity: sum{j in games} x[j] <= 4;</pre> home:  $sum\{j \text{ in games}\} h[j]*x[j] >= 2;$ away:  $sum{j in games}(1-h[j])*x[j]$ >= 1; state: sum{j in games}s[j]\*x[j] >= 2; data; param n := 8; param r :=1 3.0 2 3.7 3 2.6 4 1.8 5 1.5 6 1.3 7 1.6 8 2.0; param h:=1 1 2 1 3 1 4 0 5 0 6 0 7 0 8 0; param s:=1 0 2 1 3 1 4 1 5 0 6 0 7 0 8 1; (c) The model is an

are linear, but decision variables are binary. **2-41**. (a) How to divide funds is the issue.

ILP because all constraints and the objective

- (b)  $\max \sum_{j=1}^{n} v_j x_j$ (c)  $\min \sum_{j=1}^{n} r_j x_j$
- (d)  $\sum_{j=1}^{n} x_j = 1$
- (e)  $x_j \ge \ell_j, j = 1, ..., n$  (each category j)

## Solutions Manual for Optimization in Operations Research 2nd Edition by Rardin IBSN 9780134384559

Full Download: http://downloadlink.org/product/solutions-manual-for-optimization-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operations-research-2nd-edition-by-rardin-in-operation-in-

(g) A multiobjective LP because the 2 objectives and all constraints are linear, and all variables are continuous.

**2-42**. **(a)** The issue is which module goes to which site.

(b) If  $x_{i,j}x_{i',j'} = 1$  the *i* is at *j* and *i'* is at *j'*, so wire  $d_{j,j'}$  will be required. Summing over all possible location pairs captures the wire requirements for *i* and *i'*.

(c) min  $\sum_{i=1}^{m-1} \sum_{i'=i+1}^{m} a_{i,i'} \sum_{j=1}^{n} \sum_{j'=1}^{n} d_{j,j'} x_{i,j} x_{i',j'}$ (d)  $\sum_{j=1}^{n} x_{i,j} = 1, i = 1, \dots, m \text{ (each module } i)$ 

(e)  $\sum_{i=1}^{m} x_{i,j} \le 1, j = 1, ..., n$  (each site j) (f)  $x_{i,j} = 0$  or 1, i = 1, ..., m, j = 1, ..., n(g) Single objective INLP because the one objective is nonlinear and variables are discrete. (h) model; param m; param n; set modules := 1 .. m; set sites := 1 .. n; var x{i in modules, j in sites } binary; param a{ i in modules, ip in modules }; param d{ j in sites, jp in sites }; minimize totdist: sum{ i in modules, ip in modules: i < m and ip > i } a[i,ip] sum{j in sites, jp in sites: j < n and jp > jd[j,jp]\*x[i,j]\*x[ip,jp]; subject to alli {i in modules }: sum{ j in sites x[i,j] = 1; allj  $\{j \text{ in sites }\}:$ sum { i in modules }  $x[i,j] \le 1$ ; **2-43**.  $\max 199x_1 + 229x_2 + 188x_3 + 205x_4 180y_1 - 224y_2 - 497y_3$ , subject to,  $23x_3 + 41x_4 \le 2877y_1$ ,  $14x_1 + 29x_2 \le 2333y_2$ ,  $11x_3 + 27x_4 \le 3011y_3,$  $x_1 + x_2 + x_3 + x_4 \ge 205, y_1 + y_2 + y_3 \le 2,$  $x_1, \ldots, x_4 \ge 0, y_1, \ldots, y_3 = 0 \text{ or } 1$ **2-44**.  $\max 11x_{1,1} + 15x_{1,2} + 19x_{1,3} + 10x_{1,4} +$  $19x_{2,1} + 23x_{2,2} + 44x_{2,3} + 67x_{2,4} + 17x_{3,1} +$  $18x_{3,2} + 24x_{3,3} + 55x_{3,4}$ , subject to,  $15x_{1,1} +$  $24x_{2,1} + 17x_{3,1} \leq 7600, 19x_{1,2} + 26x_{2,2} +$  $13x_{3,2} \le 8200, 23x_{1,3} + 18x_{2,3} + 16x_{3,3} \le 6015,$ 

 $\begin{array}{l} 14x_{1,4} + 33x_{2,4} + 14x_{3,4} \leq 5000, 31x_{1,1} + 26x_{2,1} + \\ 21x_{3,1} \leq 6600, 25x_{1,2} + 28x_{2,2} + 17x_{3,2} \leq 7900, \\ 39x_{1,3} + 22x_{2,3} + 20x_{3,2} \leq 5055, \ 29x_{1,4} + \end{array}$ 

al-for-optimization-in-operations-research-2nd-edition-by-rarding  $31x_{2,4}+18x_{3,4} \leq 7777, x_{1,1}+x_{2,1}+x_{3,1} \geq 200,$   $x_{1,2}+x_{2,2}+x_{3,2} \geq 300, x_{1,3}+x_{2,3}+x_{3,3} \geq 250, x_{1,4}+x_{2,4}+x_{3,4} \geq 500, x_{j,t} \geq 0, \ j=1,\dots 3, \ t=1,\dots 4.$