CHAPTER 2. NATURE OF MATERIALS

- **2.1.** See Section 2.2.1.
- **2.2.** See Section 2.1.
- **2.3.** See Section 2.1.1.
- **2.4.** See Section 2.1.1.
- **2.5.** See Section 2.1.2.
- **2.6.** See Section 2.2.1.
- **2.7.** See Section 2.1.2.
- **2.8.** See Section 2.2.1.
- **2.9.** See Section 2.2.1.
- **2.10.** If the atomic masses and radii are the same, then the material that crystalizes into a lattice with a higher APF will have a larger density. The FCC structure has a higher APF than the BCC structure.
- **2.11.** For the face-center cubic crystal structure, number of equivalent whole atoms in each unit cell = 4

By inspection the diagonal of the face of a FCC unit cell = 4r

Using Pythagorean theory:

$$(4r)^2 = a^2 + a^2$$

$$16r^2 = 2 a^2$$

$$8r^2 = a^2$$

$$a = 2\sqrt{2}r$$

- 2.12. a. Number of equivalent whole atoms in each unit cell in the BCC lattice structure = 2
 - b. Volume of the sphere = $(4/3) \pi r^3$

Volume of atoms in the unit cell = $2 \times (4/3) \pi r^3 = (8/3) \pi r^3$

By inspection, the diagonal of the cube of a BCC unit cell

$$=4r = \sqrt{a^2 + a^2 + a^2} = a\sqrt{3}$$

a = Length of each side of the unit cell = $\frac{4r}{\sqrt{3}}$

c. Volume of the unit cell =
$$\left[\frac{4r}{\sqrt{3}}\right]^3$$

$$APF = \frac{volume \quad of \quad atoms \quad in \quad the \quad unit \quad cell}{total \quad unit \quad volume \quad of \quad the \quad cell} = \frac{(8/3)\pi \cdot r^3}{(4r/\sqrt{3})^3} = \mathbf{0.68}$$

- **2.13.** For the BCC lattice structure: $a = \frac{4r}{\sqrt{2}}$ Volume of the unit cell of iron = $\left[\frac{4r}{\sqrt{3}}\right]^3 = \left[\frac{4x0.124x10^{-9}}{\sqrt{3}}\right]^3 = 2.348 \times 10^{-29} \,\mathrm{m}^3$
- **2.14.** For the FCC lattice structure: $a = 2\sqrt{2}r$ Vol. of unit cell of aluminum = $(2\sqrt{2}r)^3 = (2\sqrt{2}x0.143)^3 = 0.06616725 \text{ nm}^3 = 6.6167 \times 10^{-29} \text{ m}^3$
- **2.15.** From Table 2.3, copper has an FCC lattice structure and r of 0.1278 nm Volume of the unit cell of copper = $(2\sqrt{2}r)^3 = (2\sqrt{2}x0.1278)^3 = 0.04723 \text{ nm}^3 = 4.723 \text{ x}10^{-29} \text{ m}^3$
- **2.16.** For the BCC lattice structure: $a = \frac{4r}{\sqrt{3}}$ Volume of the unit cell of iron = $\left[\frac{4r}{\sqrt{3}}\right]^3 = \left[\frac{4x0.124x10^{-9}}{\sqrt{3}}\right]^3 = 2.348 \times 10^{-29} \,\text{m}^3$

Density =
$$\rho = \frac{nA}{V_C N_A}$$

n = Number of equivalent atoms in the unit cell = 2

A = Atomic mass of the element = 55.9 g/mole

N_A= Avogadro's number =
$$6.023 \times 10^{23}$$

$$\rho = \frac{2x55.9}{2.348x10^{-29}x6.023x10^{23}} = 7.904 \times 10^6 \text{ g/m}^3 = 7.904 Mg/m}^3$$

2.17. For the BCC lattice structure: $a = \frac{4r}{\sqrt{2}}$

Vol. of the unit cell of molybdenum = $\left[\frac{4r}{\sqrt{3}}\right]^3 = \left[\frac{4x0.1363x10^{-9}}{\sqrt{3}}\right]^3 = 3.119 \times 10^{-29} \,\text{m}^3$

$$\rho = \frac{nA}{V_C N_A} = \frac{2x95.94}{3.119x10^{-29}x6.023x10^{23}} = 10.215 \text{ x } 10^6 \text{ g/m}^3 = \mathbf{10.215 Mg/m}^3$$

For the BCC lattice structure: $a = \frac{4r}{\sqrt{2}}$

Volume of the unit cell of the metal = $\left[\frac{4r}{\sqrt{3}}\right]^3 = \left[\frac{4x0.128x10^{-9}}{\sqrt{3}}\right]^3 = 2.583 \times 10^{-29} \,\text{m}^3$

$$\rho = \frac{nA}{V_C N_A} = \frac{2x63.5}{2.583x10^{-29}x6.023x10^{23}} = 8.163 \text{ x } 10^6 \text{ g/m}^3 = 8.163 \text{ Mg/ m}^3$$

2.19. For the FCC lattice structure: $a = 2\sqrt{2r}$

Volume of unit cell of the metal = $(2\sqrt{2}r)^3 = (2\sqrt{2}x0.132)^3 = 0.05204 \text{ nm}^3 = 5.204 \text{x} \cdot 10^{-29} \text{ m}^3$

$$\rho = \frac{nA}{V_C N_A} = \frac{4x42.9}{5.204x10^{-29}x6.023x10^{23}} = 5.475 \text{ x } 10^6 \text{ g/m}^3 = 5.475 \text{ Mg/ m}^3$$

2.20. For the FCC lattice structure: $a = 2\sqrt{2r}$

Volume of unit cell of aluminum = $(2\sqrt{2}r)^3 = (2\sqrt{2}x0.143)^3 = 0.06616725 \text{ nm}^3 = 6.6167x10^{-29} \text{ m}^3$

Density =
$$\rho = \frac{nA}{V_C N_A}$$

For FCC lattice structure, n = 4

A = Atomic mass of the element = 26.98 g/mole

 N_A = Avogadro's number = 6.023 x 10^{23}

$$\rho = \frac{4x26.98}{6.6167x10^{-29}x6.023x10^{23}} = 2.708 \times 10^6 \text{ g/m}^3 = 2.708 \text{ Mg/m}^3$$

 $2.21. \ \rho = \frac{nA}{V_C N_A}$

$$\rho = \frac{nA}{V_C N_A}$$
For FCC lattice structure, n = 4
$$V_c = \frac{4x63.55}{8.89x10^6 x6.023x10^{23}} = 4.747 \times 10^{-29} \text{ m}^3$$

APF =
$$0.74 = \frac{4x(4/3)\pi \cdot r^3}{4.747x10^{-29}}$$

$$r^3 = 0.2097 \times 10^{-29} \text{ m}^3$$

$$r = 0.128 \times 10^{-9} \text{ m} = 0.128 \text{ nm}$$

2.22. a. $\rho = \frac{nA}{V - M}$

For FCC lattice structure, n = 4

$$V_c = \frac{4x40.08}{1.55x10^6 x6.023x10^{23}} = 1.717 \times 10^{-28} \text{ m}^3$$

b. APF =
$$0.74 = \frac{4x(4/3)\pi . r^3}{1.717x10^{-28}}$$

 $r^3 = 0.7587 \times 10^{-29} \text{ m}^3$
 $r = 0.196 \times 10^{-9} \text{ m} = \textbf{0.196 nm}$

2.23.
$$\frac{\rho_1}{\rho_2} = \frac{n_1 A_1 V_{c2} N_A}{V_{c1} N_A n_2 A_2} = \frac{n_1 V_{c2}}{n_2 V_{c1}}$$
$$\frac{8.87}{\rho_2} = \frac{2 x (\frac{4r}{\sqrt{3}})^3}{4x (2r\sqrt{2})^3}$$
$$\rho_2 = 32.573 \text{ g/cm}^3$$

- **2.24.** See Section 2.2.2.
- **2.25.** See Section 2.2.2.
- **2.26.** See Section 2.2.2.
- **2.27.** See Figure 2.14.
- **2.28.** See Section 2.2.5.

2.29.
$$m_t = 100 \text{ g}$$

$$P_B = 65 \%$$

$$P_{lB} = 30 \%$$

$$P_{sB} = 80 \%$$

From Equations 2.4 and 2.5,

$$m_l + m_s = 100$$

$$30 m_l + 80 m_s = 65 \times 100$$

Solving the two equations simultaneously, we get:

 m_1 = mass of the alloy which is in the liquid phase = **30 g**

 m_s = mass of the alloy which is in the solid phase = **70** g

2.30.
$$m_t = 100 \text{ g}$$

$$P_B = 45 \%$$

$$P_{lB} = 17 \%$$

$$P_{sB} = 65 \%$$

From Equations 2.4 and 2.5,

$$m_l + m_s = 100$$

$$17 m_l + 65 m_s = 45 \times 100$$

Solving the two equations simultaneously, we get:

 m_1 = mass of the alloy which is in the liquid phase = **41.67** g

 $m_s = \text{mass of the alloy which is in the solid phase} = 58.39 \text{ g}$

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2.31. m_t = 100 \text{ g} P_B = 60 \% P_{lB} = 25 \% P_{sB} = 70 \% From Equations 2.4 and 2.5, m_l + m_s = 100 25 m_l + 70 m_s = 60 \times 100 Solving the two equations simultaneously, we get: m_l = \text{mass of the alloy which is in the liquid phase} = 22.22 g <math>m_s = \text{mass of the alloy which is in the solid phase} = 77.78 g
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2.32.
$$m_t = 100 \text{ g}$$
 $P_B = 40 \%$ $P_{IB} = 20 \%$ $P_{SB} = 50 \%$ From Equations 2.4 and 2.5, $m_l + m_s = 100$ $40 m_l + 50 m_s = 40 \times 100$ Solving the two equations simultaneously, we get: $m_l = \text{mass of the alloy which is in the liquid phase} = 33.33 \text{ g}$ $m_s = \text{mass of the alloy which is in the solid phase} = 66.67 \text{ g}$

- **2.33.** a. Spreading salt reduces the melting temperature of ice. For example, at a salt composition of 5%, ice starts to melt at -21°C. When temperature increases more ice will melt. At a temperature of -5°C, all ice will melt.
 - b. -21°C
 - c. -21°C
- **2.34.** See Section 2.3.
- **2.35.** See Section 2.3.
- **2.36.** See Section 2.4.