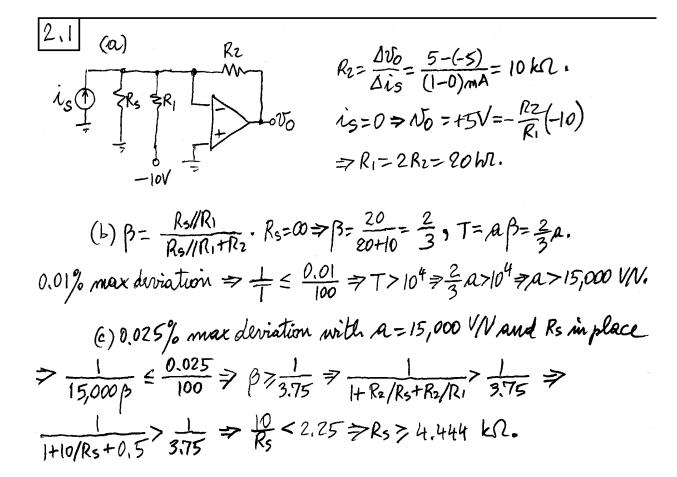
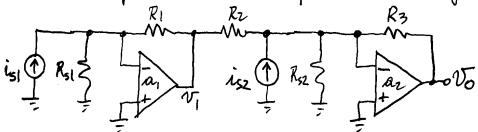
## CH. 2 – PROBLEM SOLUTIONS

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2.2 (a) Input sources must be fed to "virtual grounds":

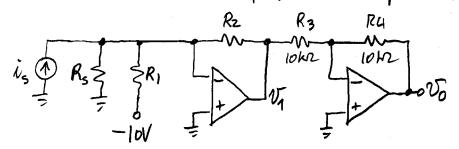


 $N_0 = -R_3 \dot{n}_{S2} - \frac{R_3}{R_2} N_1 = -R_3 \dot{n}_{S2} - \frac{R_2}{R_3} (-R_1 \dot{n}_{S1}) = A_1 \dot{n}_{S1} + A_2 \dot{n}_{S2} A_2 = R_3,$   $A_1 = \frac{R_2 R_3}{R_1} \cdot A_1 = A_2 = 10 \text{ V/mA} \Rightarrow R_3 = 10 \text{ kg} \cdot \text{Need } R_2/R_1 = 1. \text{ Pick also}$   $R_1 = R_2 = 10 \text{ kg} \cdot \text{M}.$ 

(b) 
$$\beta_1 = \frac{R_{51}}{R_{51} + R_1} = \frac{30}{30 + 10} = 0.75 \Rightarrow T_1 = A_1 \beta_1 = 10^3 \times 0.75 = 750.$$

$$N_{6}=10^{4}\left(1-\frac{1}{428.6}\right)$$
 is  $2-\frac{10^{4}}{10^{4}}\left(1-\frac{1}{428.6}\right)\left(-10^{4}\right)\left(1-\frac{1}{450}\right)$  is  $1.42 \approx 9997$  A/V,  $A_{1}=9963$  A/V.

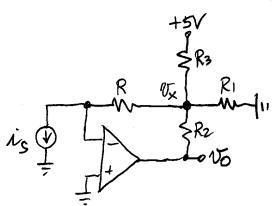
2.3 Need an I-V converter stage with offset, followed by an inverting stage to ensure proper output polarity.



 $\Delta i_{s} = (20-4) \text{ mA} = 16 \text{ mA}, \ \Delta v_{1} = -\Delta v_{0} = -8 \text{ V}, \ R_{z} = \left| \frac{\Delta V_{1}}{\Delta i_{s}} \right| = \frac{8}{16} = 500 \text{ } \Omega.$   $i_{s} = 4 \text{ mA} \Rightarrow v_{0} = 0 \Rightarrow v_{1} = 0 \Rightarrow i_{R_{z}} = 0 \Rightarrow i_{R_{1}} = i_{s} = 4 \text{ mA} \Rightarrow$   $R_{1} = 10/4 = 2.5 \text{ kg}.$ 

2.5

(a)  $A = \Delta V_0/\Delta i_S = [4-(-4)]/(10\mu A) = 800 \text{ kg. Use a high-somoitivity}$ 



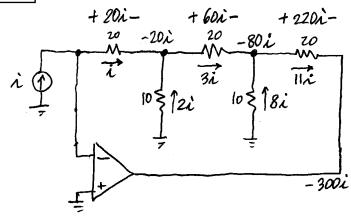
+5V I-V converter with  $R_3$  and the  $R_3$  and the  $R_3$   $R_3$   $R_4$   $R_5$   $R_5$   $R_5$   $R_5$   $R_6$   $R_6$   $R_6$   $R_6$   $R_6$   $R_7$   $R_7$   $R_8$   $R_8$   $R_8$   $R_8$   $R_8$   $R_9$   $R_9$ 

When is=10 MA we have  $0x = 0x + Ris = 0 + 10^{5} \times 10 \times 10^{6} = 1V$  & we want 00 = +4V. KCL@ 0x:  $\frac{5-1}{R_3} + \frac{4-1}{R_2} = 0.01 + \frac{1}{R_1}$ . Let  $R_1 = 1 \text{ k}\Omega$ .

Substituting,  $\frac{4}{R_3} + \frac{3}{0.8R_3} = 1.01 \Rightarrow R_3 = 7.673 \text{ kg}, R_2 = 6.138 \text{ kg}.$ 

 $\beta = \frac{R_3//R_1}{R_3//R_1 + R_2} = \frac{1}{1 + R_2/R_3 + R_2/R_1} = \frac{1}{1 + 0.8 + 6.138} = \frac{1}{8} = \frac{0.1}{100} = 10^{-3}$   $\Rightarrow T = AR \Rightarrow 10^3 \le A/8 \Rightarrow A \geqslant 8,000 \text{ V/V}.$ 





Start out a left, and work your way Toward the right via repeated application of SR, kVL, and kCl to get A=\frac{No}{iI} = -300 V/mA.

Shunt a input => Ri = \frac{\tio}{1+T}.

20 Start a right and work your way toward the left:

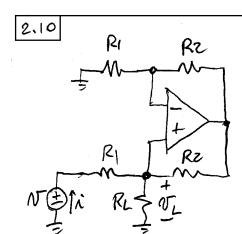
= \( \io = \{ \left[ (20/10) + 20 \right] // 10\} + 20 = 27.3 kr. \)

T=aB=104/1=909; Ri=(27.3×103)/909=30 m.s.

[2.7] (a)  $i_0 = i_{R_2} + i_{R_3} = i_{R_1} + i_{R_3} = \frac{v_T}{R_1} + \frac{v_T}{R_2} = \frac{v_T}{R_1} + \frac{v_T}{R_3} = \frac{v_T}{R_1} + \frac{v_T}{R_2} =$ 

[2.8]
(a)  $\beta = \sqrt{2}$ ,  $T = \alpha \beta = 500$ ,  $V_0 = -\frac{100}{100} \frac{1}{1+\sqrt{500}} V_1 = -\frac{500}{501} V_2$ .  $V_1 = \frac{1}{100} V_2$ ,  $V_0 = \frac{1}{1$ 

2.9 Eq. (2.7) gives lim  $R_0 = \infty$ , so (c) is correct. (a) is wrong because it ignores negative feedback. (b) is wrong because the op samp keeps a virtual short between  $N_N$  and  $N_p$ , not between  $N_N$  and  $N_p$ , and  $N_p$ .

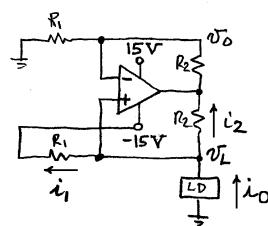


(a) Apply at the voltage V.  $V_L = R_L \dot{N}_L = R_L \frac{N}{R_I}$   $\dot{N} = \frac{V - N \dot{L}}{R_I} = \frac{1 - R_L / R_I}{R_I} V$   $R_i = N \dot{R}_i = R_I / (1 - R_L / R_I)$ . (b)  $R_L = R_I \Rightarrow V_L = R_L \frac{V}{R_I} = V \Rightarrow \dot{N} = 0$ 

=7Ri=00.  $R_{L}< R_{I} \Rightarrow V_{L}< V \Rightarrow i$  flowing toward the right  $\Rightarrow Ri>0$   $R_{L} \Rightarrow R_{I} \Rightarrow V_{L} > V \Rightarrow i$  flowing toward the left  $\Rightarrow$  negative Ri.

Ro=10 1+Tec, Vio= lim Ro = R1/1R2. Output port open-circuited > VD=0 > 15=0 Toc = - Vipor =0. Output port shortaranted > VD = - KI VT RZ VR= AVO = - A OT Tsc = - UR = R - 1+R2/R1. Ro-(RillR2) (I+ 1+RedRi). (b) io (NI=0)= = -1.0 mA. Ro=(103/103) (1+ 104)= 2.5 M.R. Use Norton equivalent:  $1.0 + \frac{VL}{R_0} + i_0 = 0$   $\Rightarrow i_0 = -1.0 \text{ mA} - \frac{VL}{2.5 \text{ mSi}}$   $i_0(v_1 = 2.71)$   $i_0 = -10^3 - \frac{5}{2.5 \times 10^6} = -1.002 \text{ mA}$ 10(N==2.5V)=-10-3+ 2.5 25x10-6=-0.999 mA.

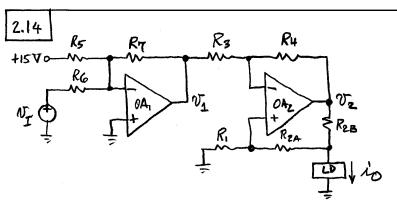
2.12 R= 15/1.5 = 10.0 kl, 1%; R= 0.3 R1.



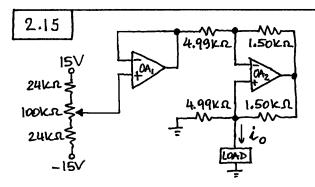
Use  $R_2 = 2.00 \text{ k/L}, 1\%$ . Then,  $V_0 = (1+2/10)V_L$ = 1.2  $V_L$ .

- (a)  $V_L = -2 \times 1.5 = -3 \text{ V}; V_0 = -3.6 \text{ V};$   $i_1 = [-3 (-15)]/10 = 1.2 \text{ mA}; i_2 = [-3 (-3.6)]/2 = 0.3 \text{ mA}; clearly, <math>i_0 = i_1 + i_2 = 1.2 + 0.3 = 1.5 \text{ mA}.$ (b)  $V_L = -9 \text{ V}, V_0 = -10.8 \text{ V}, i_1 = 0.6 \text{ mA},$   $i_2 = 0.9 \text{ mA}.$
- (c) With the athode at ground, the zener gives  $V_L = -5 \text{ V}$ , so  $N_0 = -6 \text{ V}$ , i, =1 mA,  $N_2 = 0.5 \text{ mA}$ .
  - (d) Vo=VL=0, i,=1.5mA, iz=0.
- (e) With a 10-kl boad the op amp saturates at  $-13 \, \text{V}$ . By kCL,  $(0-v_L)/10 = (v_L + 15)/10 + (v_L + 13)/2$ , or  $v_L = -80/7 \, \text{V}$ . So,  $i_0 = 1.143 \, \text{mA}$ ,  $i_1 = 0.357 \, \text{mA}$ ,  $i_2 = 0.786 \, \text{mA}$ . Because of saturation we have  $i_1 + i_2 = i_0 \neq 1.5 \, \text{mA}$ .

2.13 Superposition:  $v_0 = -\frac{R_4}{R_3}v_1 + \left(1 + \frac{R_4}{R_3}\right)v_L$ ; kcl:  $v_1 = \frac{v_2 - v_L}{R_1} + \frac{v_0 - v_L}{R_2}$   $v_1 = \frac{v_2}{R_1} + \frac{v_0 - v_L}{R_2} - \left(\frac{1}{R_1} + \frac{1}{R_2}\right)v_L$   $v_2 = \frac{v_2}{R_1} - \frac{R_4}{R_2R_3}v_1 - v_L\left(\frac{1}{R_1} + \frac{1}{R_2} - \frac{R_4}{R_2}R_3\right)$   $= \frac{1}{R_1}\left(v_2 - \frac{R_1}{R_2}\frac{R_4}{R_3}v_1\right) - \frac{v_1}{R_2}\left(\frac{R_2}{R_1} - \frac{R_4}{R_3}\right)$   $v_2 = \frac{1}{R_1}\left(v_2 - \frac{R_1}{R_2}\frac{R_4}{R_3}v_1\right) - \frac{v_1}{R_2}\left(\frac{R_2}{R_1} - \frac{R_4}{R_3}\right)$   $v_2 = \frac{1}{R_1}\left(v_2 - \frac{R_4}{R_2}\frac{R_4}{R_3}v_1\right) - \frac{v_1}{R_2}\left(\frac{R_2}{R_1} - \frac{R_4}{R_3}\right)$   $v_2 = \frac{1}{R_1}\left(v_2 - \frac{R_4}{R_2}\frac{R_4}{R_3}v_1\right) - \frac{v_1}{R_2}\left(\frac{R_2}{R_1} - \frac{R_4}{R_3}\right)$   $v_2 = \frac{1}{R_1}\left(v_2 - \frac{R_4}{R_2}\frac{R_4}{R_3}v_1\right) - \frac{v_1}{R_2}\left(\frac{R_2}{R_1} - \frac{R_4}{R_3}\right)$   $v_3 = \frac{1}{R_1}\left(v_2 - \frac{R_4}{R_2}\frac{R_3}{R_3}v_1\right) - \frac{v_1}{R_2}\left(\frac{R_2}{R_1} - \frac{R_4}{R_3}\right)$   $v_3 = \frac{1}{R_1}\left(v_2 - \frac{R_4}{R_2}\frac{R_3}{R_3}v_1\right) - \frac{v_1}{R_2}\left(\frac{R_2}{R_3} - \frac{R_4}{R_3}v_1\right)$   $v_4 = \frac{1}{R_1}\left(v_2 - \frac{R_4}{R_2}\frac{R_3}{R_3}v_1\right) - \frac{v_1}{R_2}\left(\frac{R_2}{R_3} - \frac{R_4}{R_3}v_1\right)$   $v_4 = \frac{1}{R_1}\left(v_2 - \frac{R_4}{R_2}\frac{R_3}{R_3}v_1\right) - \frac{v_1}{R_2}\left(\frac{R_2}{R_3} - \frac{R_4}{R_3}v_1\right)$   $v_4 = \frac{1}{R_1}\left(v_2 - \frac{R_4}{R_2}\frac{R_4}{R_3}v_1\right) - \frac{v_1}{R_2}\left(\frac{R_2}{R_3} - \frac{R_4}{R_3}v_1\right)$   $v_4 = \frac{1}{R_1}\left(v_2 - \frac{R_4}{R_2}\frac{R_4}{R_3}v_1\right) - \frac{v_1}{R_2}\left(\frac{R_2}{R_3} - \frac{R_4}{R_3}v_1\right)$   $v_4 = \frac{1}{R_1}\left(v_2 - \frac{R_4}{R_2}\frac{R_4}{R_3}v_1\right) - \frac{v_1}{R_2}\left(\frac{R_4}{R_3} - \frac{R_4}{R_3}v_1\right)$   $v_4 = \frac{1}{R_1}\left(v_2 - \frac{R_4}{R_2}\frac{R_4}{R_3}v_1\right) - \frac{v_1}{R_2}\left(\frac{R_4}{R_3} - \frac{R_4}{R_3}v_1\right)$   $v_5 = \frac{1}{R_1}\left(v_2 - \frac{R_4}{R_3}\frac{R_4}{R_3}v_1\right) - \frac{v_1}{R_2}\left(\frac{R_4}{R_3}v_1\right)$   $v_5 = \frac{1}{R_1}\left(v_2 - \frac{R_4}{R_2}\frac{R_4}{R_3}v_1\right) - \frac{v_1}{R_2}\left(\frac{R_4}{R_3}v_1\right)$   $v_5 = \frac{R_4}{R_2}\left(\frac{R_4}{R_3}v_1\right) - \frac{v_1}{R_3}\left(\frac{R_4}{R_3}v_1\right)$   $v_5 = \frac{R_4}{R_3}\left(\frac{R_4}{R_3}v_1\right) - \frac{v_1}{R_3}\left(\frac{R_4}{R_3}v_1\right)$   $v_5 = \frac{R_4}{R_3}\left(\frac{R_4}{R_3}v_1\right) - \frac{v_1}{R_3}\left(\frac{R_4}{R_3}v_1\right)$   $v_5 = \frac{R_4}{R_3}\left(\frac{R_4}{R_3}v_1\right) - \frac{v_1}{R_3}\left(\frac{R_4}{R_3}v_1\right)$   $v_5 = \frac{v_5}{R_3}\left(\frac{R_4}{R_3}v_1\right) - \frac{v_5}{R_3}$ 



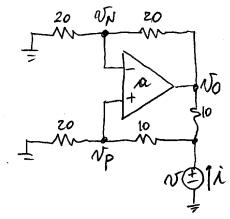
Let  $R_1 = R_3 = R_4 = 10 \text{ kr}$ . Assume a maximum drop of 2V across  $R_{2B}$ , so  $R_{2B} = 2/20 = 100 \Omega$ . Then,  $R_{2A} = 10 \text{ k} \Omega - 100 \Omega = 9.9 \text{ k} \Omega$ .  $V_{\underline{1}} = 0 \Rightarrow V_{1} = -(R_{1}/R_{5})15 = -0.4 \Rightarrow R_{5}/R_{1} = 37.5$   $V_{\underline{1}} = 10V \Rightarrow V_{1} = -0.4 - (R_{1}/R_{6})10 = -2 \Rightarrow R_{6}/R_{1} = 6.25$ . Use  $R_{1} = 2 \text{ k} R_{1}$ ,  $R_{6} = 12.5 \text{ k} R_{1}$ ,  $R_{5} = 75 \text{ k} R_{2}$ .



OA, provides a variable voltage from -10V to +10V, which OA, converts to a variable current from -2mA to +2mA.

V6 = (1+ R4) VP  $V_{\mathbf{P}} = \frac{K_{2}AV_{\mathbf{I}} + K_{1}V_{\mathbf{L}}}{R_{1} + R_{2}A}$ is= RVI - RVI, where R= R3 R2B (R1+REA), R0= R2B (1+ R2A/R1)
R3 (R2A+R2B)+R4R2A, R0= R1/R2-(R2A+R2B)/R1 To make Ro = 00 improse R4/R3 = R2/R1, where Rz= Rza+ RzB. This gives  $R = \frac{R_3 R_{2B} (R_1 + R_{2A})}{R_{II} (R_1 + R_{2A})} = \frac{R_3}{R_{II}} R_{2B} \Rightarrow \frac{1}{R} = \frac{R_4 / R_3}{R_{--}}$ (b) Imposing 10 = 13 - (R4/R3)10 gives R4/R3=0.3. Let R1=R3=100 ks2, R4= REATREB = 30.1 K. Then, imporing (R4/R3)/R2B =0.301/R2B=1 mA/V gires R2B=301 SZ. Firmally, R24=30.1-0.301=29.8 W. (me 30.1 kr, 1%).

Test method



$$\nabla_{p} = \frac{2}{3} \nabla, \quad \nabla_{N} = \frac{1}{2} \nabla_{0}, \quad \nabla_{\theta} = \mathcal{A} \left( \nabla_{p} - \nabla_{N} \right) \\
\nabla_{0} = \mathcal{A} \left( \frac{2}{3} \nabla - \frac{1}{2} \nabla_{0} \right) \Rightarrow \nabla_{\theta} = \frac{4 \pi \alpha}{6 + 3 \alpha} \nabla \\
\dot{\iota} = \frac{\nabla}{20 + 10} + \frac{\nabla - \nabla_{0}}{10} = \mathcal{V} \left( \frac{1}{30} + \frac{1}{10} - \frac{1}{10} \frac{4 \alpha}{6 + 3 \alpha} \right)$$

$$\hat{l} = \frac{9}{30} \left[ 1 + 3 - \frac{12a}{6 + 3a} \right] = \frac{24v}{30(6 + 3a)}$$

$$\hat{J} \hat{\lambda} = \frac{9}{30} \left[ 1 + 3 - \frac{12a}{6 + 3a} \right] = \frac{24v}{30(6 + 3a)}$$

$$R_0 = \frac{v}{\hat{k}} = \frac{30(6+3a)}{24} = (7.5kg)(1+\frac{a}{2})$$
  
=  $(7.5kg)(1+\frac{104}{2}) = 37.5 M.Q.$ 

Voo = (20+10)//10 = 7.5h2. PORT ofen-circuited = ND=0 = VR=0 > Toc=-UR = 0

PORT short-circuited >

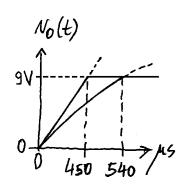
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2.18 Work with Norton equivalent.



(a) 
$$R_0 = \infty$$
,  $N_c = \frac{\dot{x}_0}{C} t = \frac{10^3}{10^{-7}} t = 10^4 t$   
 $N_0(t) = \left(1 + \frac{R_4}{R_3}\right) N_c(t) = 2 \times 10^4 t$ , ramp till

of amp caturates at 9 V. Impose 9 = 2×104 and get t = 450 µs.



(b) Ry=1.8 kp. 
$$\Rightarrow$$
 Ro=  $\frac{R_z}{R_z/R_1-R_4/R_3} = \frac{2}{1-0.9} = 20 \text{ kp.}$   
 $\Rightarrow$  exponential xsient with  $9 = 80 = 20 \text{ ms}$   
and  $10 = 10 = 20 \text{ V} \Rightarrow 10 = 10 = 18/2 = 10 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100 = 100$ 

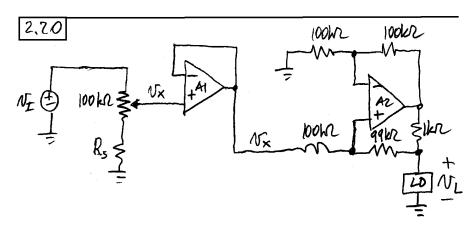
2.19 Work with Norton equivalent.  $R_4 = 2.2 \text{k/l} \Rightarrow$   $R_0 = \frac{R_2}{R_2/R_1 - R_4/R_3} = \frac{2}{1 - 1.1} = -20 \text{ k/l} \Rightarrow$ io Profic ic ic=io- $\frac{\sqrt{c}}{2}$ =10<sup>-3</sup>- $\frac{\sqrt{c}}{20 \times 10^3}$ =  $\frac{d\sqrt{c}}{dt} \Rightarrow$ 

 $20 + v_c = 20 \times 10^3 \times 10^{-6} \frac{dv_c}{dt} = (20 \text{m/s}) \frac{dv_c}{dt}$ 

Assume solution of the type Nc = Aest+B:

$$20+Ae^{5t}+B=(2ms)sAe^{st} \Rightarrow B=-20, s=1/(20ms)=50, so$$
  
 $N_{c}(k)=Ao^{50k}-20. N_{c}(0)=0 \Rightarrow A=20 \Rightarrow N_{c}=(20v)(e^{50t}-1).$ 

 $V_0(t) = (1+h_{Ks})V_0(t) = 42(e^{50t}-1)$ . Impose  $9 = 42(e^{50t}-1) \Rightarrow t = 1.7 \text{ ms}$ 



Use variable input attenuator to implement  $0.(V_{L} \leq U_{X} \leq V_{L})$ , and then use follower  $A_{1}$  to buffer  $V_{X}$  to the Howland pump with zero resistance to avoid disturbing the resistance ratios. Wiper down  $\geqslant 0.1 = R_{S}/(100 + R_{S}) \Rightarrow R_{S} = 11.1 \text{ kr. } i_{O} = \frac{V_{X}}{1 \text{ kr.}}$ 

2.21 (a) Denote the output of OA1 as  $v_{01}$ , and that of  $0A_2$  as  $v_{02}$ . By mispertion, we have  $v_{02} = v_L$ . By the superposition principle,  $v_{01} = -\frac{R_4}{R_3}v_1 + \left(1 + \frac{R_4}{R_3}\right) \frac{R_2v_2 + R_1v_L}{R_1 + R_2}$   $= \frac{1 + R_4/R_3}{1 + R_1/R_2}v_2 - \frac{R_4}{R_3}v_1 + \frac{1 + R_4/R_3}{1 + R_2/R_1}v_L.$   $i_0 = \frac{v_{01} - v_L}{R_5} = A_2v_2 - A_1v_1 - \frac{1}{R_0}v_L, \text{ where}$   $A_2 = \frac{1 + R_4/R_3}{1 + R_1/R_2}v_5, A_1 = \frac{R_4}{R_3}v_5, \text{ and}$   $v_{02} = \frac{1}{R_5}\left(1 - \frac{1 + R_4/R_3}{1 + R_2/R_1}\right) = \frac{1}{(1 + R_2/R_1)R_5}\left(\frac{R_2}{R_1} - \frac{R_4}{R_3}\right)$ 

To make  $R_0 \rightarrow 00$  impose  $R_4/R_3 = R_2/R_1$ , after which it is readily seen that  $A_1 = A_2 = \frac{R_2/R_1}{R_5}$ .

In purmmary, imposing  $R_4/R_3 = R_2/R_1$  gives  $i_0 = Av_1 - f_0v_L$ ,  $A = \frac{R_2/R_1}{R_5}$ ,  $v_1 = v_2 - v_1$ ,  $R_0 = 00$ .

(b) of the resistances are mismatched, A1 and A2 will also be mismatched, so we no longer have true difference operation. Writing  $R_0 = \frac{(1+R_2/R_1)R_5}{R_2/R_1-(R_2/R_1)(1-\epsilon)} = (1+\frac{R_2}{R_1})\frac{R_5}{\epsilon}$  gives, for 1% resistors,  $|R_0| \ge 25(1+R_2/R_1)R_5$ .

2.22 (a) Denote the output of  $OA_1$  as  $V_{01}$ , that of  $OA_2$  as  $V_{02}$ . By  $OA_2$ 's action,  $V_{01} = V_L$  and  $V_{02} = V_L + R_5 \dot{n}_0$ . By the superposition principle,  $V_{01} = -\frac{R_4}{R_3} V_{I} + \left(1 + \frac{R_4}{R_3}\right) \frac{R_1}{R_1 + R_2} \left(V_L + R_5 \dot{n}_0\right) = V_L$ . Solving for  $\dot{n}_0$  gives  $\dot{n}_0 = AV_I - \left(1/R_0\right) V_L$ ,  $A = \frac{1 + R_2/R_1}{1 + R_4/R_3} \frac{R_4/R_3}{R_5}$ ,  $R_0 = \frac{\left(1 + R_4/R_3\right) R_5}{R_2/R_1 - R_4/R_3}$ . Duponing  $R_4/R_3 = R_2/R_1$  gives  $R_0 = \omega$  and  $A = \frac{(R_2/R_1)/R_5}{R_2/R_1 - (R_2/R_1)(1-\varepsilon)}$ .

(b) Writing  $R_0 = \frac{\left(1 + R_2/R_1\right) R_5}{R_2/R_1 - (R_2/R_1)(1-\varepsilon)}$ 

2.23 (a) Denote the outputs of  $OA_1$  and  $OA_2$  as  $VOA_1$  and  $VOZ_2$ . We have  $VOZ_2 = -VOA_1 = -\left[-V_1 - (R_1/R_2)V_1\right] = V_1 + (R_1/R_2)V_1$ ; io =  $\frac{VOZ_2 - VI_2}{R_3} - \frac{VI_2}{R_2} = \frac{VI_2}{R_3} - V_1 \left[\frac{1}{R_3} + \frac{1}{R_2} - \frac{R_1/R_2}{R_3}\right]$ , or  $IO = AV_1 - \frac{1}{R_0}V_1$ ,  $A = \frac{1}{R_3}$ ,  $RO = \frac{R_2R_3}{R_2 + R_3 - R_1}$ . To achieve RO = OO, impose  $R_2 + R_3 = R_1$ .

(b) To find the effect of mismatches upon RO, apply a test voltage at the output:

RIA RIB RIC R3

$$i = \frac{V}{R_2} + \frac{V - (R_{1A}R_{1C}/R_{2}R_{1B})V}{R_3}$$

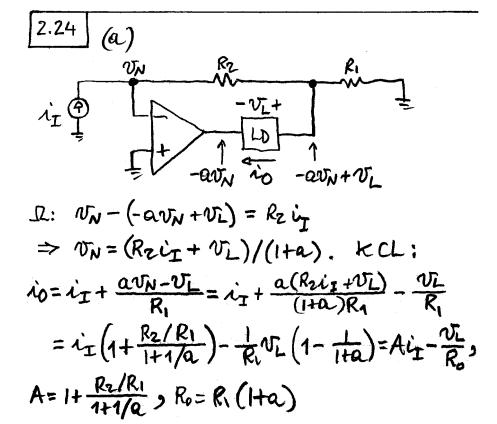
$$= \mathcal{V}\left[\frac{1}{R_2} + \frac{1}{R_3} - \frac{R_{1A}\left(R_{1C}/R_{1B}\right)}{R_2 R_3}\right]$$

Rows maximized when Rz, Rz, and R1B are maximized, and R1A and R1C arl minimized.

For 1% resistors, rewrite as

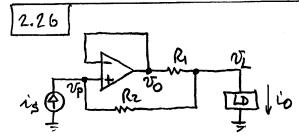
$$R_{0(\text{max})} = \frac{(R_{2} \times R_{3}) \cdot 1.01^{2}}{(R_{2} + R_{3}) \cdot 1.01 - (R_{2} + R_{3}) \cdot 0.99 \cdot (0.99/1.01)}$$

$$\stackrel{\sim}{=} 25 \frac{R_{3}}{1 + R_{3} / R_{2}}.$$

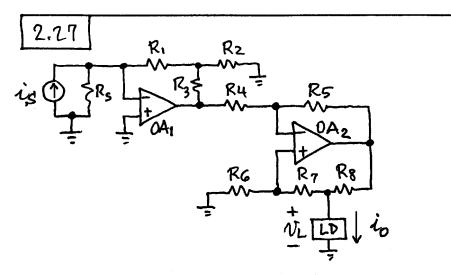


(b) Use  $R_1 = 2 kR$ ,  $R_2 = 18 kR$ . Aideal = 10 A/A; Aactual = 1+9/(1+1/200,000) = 9.999955; gain error = -0.00045%.  $R_0 \cong 2 \times 10^3 \times (1+200,000) = 400 Msl$ . 2.25 The op amp Keeps  $V_0 = V_N = V_P$ . By the superposition principle,  $V_P = (R_S/R_Z)i_S + \frac{R_S}{R_S + R_Z} V_L$ . By kCL,  $\hat{N}_0 = (\hat{V}_P - \hat{V}_L)/(R_1||R_Z)$ . Substituting,  $\hat{I}_0 = \frac{R_S//R_Z}{R_1/|R_Z|}i_S - \frac{V_L}{R_1/|R_Z|} \left[1 - \frac{R_S}{R_S + R_Z}\right] = Ai_S - \frac{V_L}{R_0}$ ,  $A = \frac{1 + R_2/R_1}{1 + R_2/R_S}$ ,  $R_0 = \frac{R_S + R_Z}{1 + R_2/R_1}$ .

For Rs -> as we get A=1+ Rz/R, and Ro=00.



 $V_{P} = V_{L} + R_{2}i_{S}$ ;  $V_{0} = A(V_{P} - V_{0}) \Rightarrow V_{0} = \frac{a}{Ha}V_{P}$   $V_{0} = \frac{a}{Ha}(V_{L} + R_{2}i_{S})$ .  $i_{0} = i_{S} + \frac{V_{0} - V_{L}}{R_{1}} \Rightarrow$   $i_{0} = i_{S} + \frac{1}{R_{1}}[\frac{a}{Ha}V_{L} - V_{L} + \frac{a}{Ha}R_{2}i_{S}] = Ai_{S} - \frac{1}{R_{0}}V_{L}$ ,  $A = 1 + (R_{2}/R_{1})/(1+1/a)$ ,  $R_{0} = R_{1}(1+a)$ .

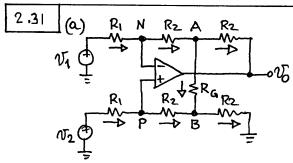


Choose the T-V converter components for a 10-V full scale at  $0A_1$ 's output. Thus, let  $R_1 = 1M\Omega$ ,  $R_2 = 1k\Omega$ ,  $R_3 = 100 k\Omega$ . io(mex) =  $10^5 \times 100 \times 10^{-9} = 10 \text{mA}$ . Disposing  $R_8 = 500 \text{ Tr}$  yields a voltage compliance of  $10-0.5 \times 10 = 5 \text{ V}$ . Finally, let  $R_4 = R_5 = R_6 = 100 \text{ kR}$ ,  $R_7 = 99.5 \text{ kD}$ .

2.28  $R_1$   $R_2$   $V_1$   $V_2$   $V_3$   $V_4$   $V_5$   $V_6$   $V_7$   $V_8$   $V_8$   $V_8$   $V_8$   $V_8$   $V_8$   $V_8$   $V_9$   $V_9$ 

2.29 The output of OA, is Ny = - RZ V2 - Ry N4. By the curresposition principle, で=-KFV、- KFV。- KFV= = RFV2 + RFV1 - RFV1 - RFV3. The circuit sums the even-numbered inputs with positive gains, and the odd-numbered inputs with negative fains. Since the summing junctions of both of amps are at virtual ground, leaving an input floating has no effect. By contrast, learning any input floating in Fif. P1.31 affects the output because in general UN = VO + 0.

[2.30] Applying a test voltage is between the inputs of Fig. 2.14a yields, by the virtual short concept,  $i=v/(R_i+O+R_i)=v/2R_1$ . So,  $Rid=2R_1$ . In response to an input test voltage is, the  $R_1$  resistances in Fig. 2.14(b) will draw the same current  $v/(R_i+R_2)$ , so  $i=2v/(R_i+R_2)$ , or  $Ric=v/i=(R_i+R_2)/2$ .



KCL at N: 
$$\frac{\sqrt{1-VN}}{R_1} = \frac{\sqrt{N-VA}}{R_2}$$

KCL at P; 
$$\frac{v_2-v_p}{R_1} = \frac{v_p-v_B}{R_2}$$

$$V_A - V_B = (R_2/R_1)(V_2 - V_1)....(1)$$

KCL at A: 
$$\frac{V_1 - V_A}{R_1 + R_2} = \frac{V_A - V_B}{R_G} + \frac{V_A - V_O}{R_2}$$
.

KCL at B: 
$$\frac{\overline{V_2} - \overline{V_B}}{R_1 + R_2} + \frac{\overline{V_A} - \overline{V_B}}{R_G} = \frac{\overline{V_B}}{R_2}$$
. Subtracting,

$$\frac{(\mathcal{V}_2 - \mathcal{V}_1) + (\mathcal{V}_A - \mathcal{V}_B)}{R_1 + R_2} + 2 \frac{\mathcal{V}_A - \mathcal{V}_B}{R_G} = \frac{(\mathcal{V}_B - \mathcal{V}_A) + \mathcal{V}_O}{R_2}.$$

Combining with Eq. (1),

$$(v_2-v_1)(\frac{1+R_2/R_1}{R_1+R_2}+2\frac{R_2/R_1}{R_6}+\frac{1}{R_1})=\frac{v_6}{R_2}$$

Solving for  $V_0$  and simplifying,  $V_0 = 2 \frac{R^2}{R_1} (1 + \frac{R^2}{R_2}) (V_2 - V_1)$ .

(b) Let 
$$R_G = 100 \text{k}\Omega$$
 pot in series with a 5-k  $\Omega$  resistor. Then,  $100 = 2(R_2/R_1)(1+R_2/5)$  and  $10 = 2(R_2/R_1)[1+R_2/(100+5)]$ . Dividing,  $100/10 = (1+R_2/5)/(1+R_2/105)$ . Solving,  $R_2 = 85.9 \text{k}\Omega$ . Back substituting yields  $R_1 = 31.24 \text{k}\Omega$ . Use  $R_1 = 31.6 \text{k}\Omega$ ,  $R_2 = 86.6 \text{k}\Omega$ ,  $R_G = 100 \text{k}\Omega$  pot  $+ 4.99 \text{k}\Omega$ , all  $1\%$ .

 $\begin{array}{c|c} \hline 2.32 & \text{(a)} \ \mathcal{V}_{02} = -\left(R_3/R_G\right) \mathcal{V}_0. \text{ Superposition:} \\ \mathcal{V}_{P1} = \frac{R_2 \mathcal{V}_2 + R_1 \mathcal{V}_{02}}{R_1 + R_2}. \text{ Voltage dividev:} \ \mathcal{V}_{N1} = \\ \left[R_2/(R_1 + R_2)\right] \mathcal{V}_1. \text{ Eliminating Vo2 and letting} \\ \mathcal{V}_{N1} = \mathcal{V}_{P1} \text{ gives } \mathcal{V}_0 = \frac{R_2}{R_1} \frac{R_G}{R_3} \left(\mathcal{V}_2 - \mathcal{V}_1\right). \\ \begin{pmatrix} 1 & 1 & 2 & 2 & 2 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} & \begin{pmatrix} 1 & 1 & 2 & 2 & 2 \\ \end{pmatrix} &$ 

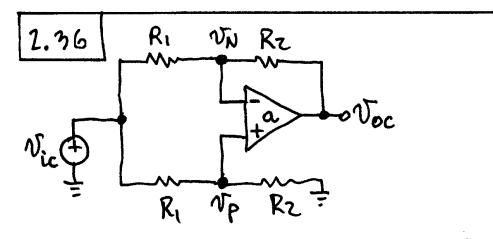
(b) Let  $R_1 = R_2 = 10 \text{ k.r.}$ . Then,  $A = R_G/R_3$ . Let  $R_3 = 1 \text{ k.r.}$  and let  $R_G$  be a 100-k.r. pot in Series with a 1-k.r. resistor. Then, A(min) = 1 V/V,  $A(\text{max}) = (1+100)/1 \approx 100 \text{ V/V}$ .

[2.33] (a)  $(V_1+V_2)/2 = 10 \text{ con } 2\pi 60t \ V$ ;  $V_2-V_1 = 0.01 \text{ con } 2\pi 10^3t \ V$ ;  $A_{dm} = 2/0.01 = 200$ V/V;  $A_{cm} = 0.1/10 = 0.01 \ V/V$ ;  $CMRR = 20 \text{ log}_{10} (200/0.01) = 86 \text{ dB}$ .

(b)  $(V_1+V_2)/2 = 10.005 \cos 2\pi 60t \ V_3$   $V_2-V_1 = -0.01 \, \text{min} \ 2\pi 60t + 0.01 \, \text{sin} \ 2\pi 10^3 t \ V_3$ Adm =  $2.5/0.01 = 250 \, \text{V/V}$ . At 60 Hz, we have  $0.5 = 250 \times (-0.01) + \text{Acm} \times 10.005$ , or  $\text{Acm} = 0.3 \, \text{V/V}$ ; CMRR =  $20\log_{10}(250/0.3) = 58.4 \, \text{dB}$ .

[2.34] Adm  $\cong (100 \text{ kR})/(1 \text{ kg}) = 100 \text{ V/V} = 40 \text{ dB}$ . To find Acm, the the inputs together and apply a common argual. Then,  $Acm = -\frac{99.7}{1.01} + (1 + \frac{99.7}{1.01}) \frac{102}{102 + 0.995} = 0.0367 \text{ V/V}$   $= -28.7 \text{ dB}. \text{ CMRR} \cong 40 - (-28.7) = 68.7 \text{ dB}.$ 

[2.35]  $|A_{dm}| = 10^{3} \text{V/V} \notin \text{CMRR} = 10^{5} \Rightarrow |A_{cm}| = 10^{2} \text{V/V}.$   $|V_{id}| = |V_{2} - V_{1}| = 2mV; \quad |V_{ic}| = (|V_{1} + |V_{2}|)/2 = 4V;$   $|V_{od}| = |V_{3} \times 2 \times |V_{3}| = 2V; \quad |V_{oc}| = 10^{-2} \times 4 = 0.04V.$   $|V_{od}| = |V_{oc}| = |V_{oc}| = 2\%.$ 



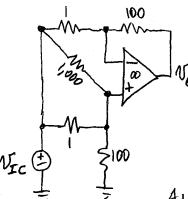
 $\sqrt{SC} = A(V_P - V_N) = A \left[ \frac{Rz}{R_1 + Rz} V_{ic} - \frac{RzV_{ic} + R_1 V_{oc}}{R_1 + Rz} \right] \\
 = A \left[ \frac{Rz}{R_1 + Rz} V_{ic} - \frac{Rz}{R_1 + Rz} V_{oc} \right]$ 

₹ Voc (1+aβ)=0 ⇒ Voc = 0 regardles of Vic ⇒ CMRR = ∞. Intuitively: Voc can only be zero. Suppose voc was positive. Then, vo would be > vp, implying that vo=a(vp-vw) would have to swing negative, a contradiction.



Tie mputs together and drive them with a common morde

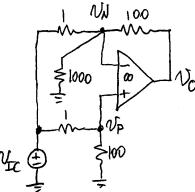
voltage NIc, and find Voc.



(a) 
$$R_1 = 1 h\Omega$$
,  $R_2 = K_4 = 100 k\Omega$ ,  $R_3 = 1/1,000$   
=  $\frac{1000}{1001} k\Omega$ . Superposition:

$$Noc = NEC \left(-100 + 101 \frac{1001}{1011}\right) = \frac{NEC}{1011} \Rightarrow Acm = \frac{1}{1011}$$

Adm = 100 V/V; CMRR = 20le 100/(1/1011) = 100.1 dB.



(b) Superposition:

$$NOC = -\frac{100}{1}NIC + (1 + \frac{100}{1000/1001}) NIC$$
  
=  $NIC (-100 + 101.1) NIC = 1.1 NIC >$ 

Acm=1.1V/V. CMRR=20lg/100/1.1=39.17dB

$$\frac{V_2 - V_P}{I} = \frac{V_P}{100} + \frac{V_P - V_O}{1000}$$

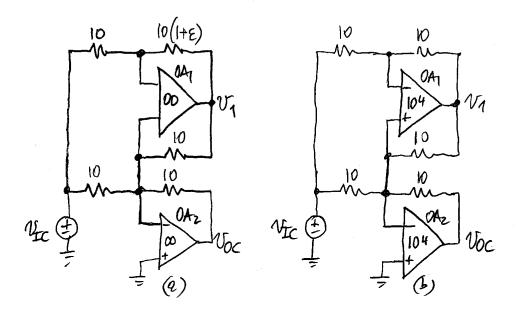
1000×101 Vz-1011×1004=910 00

$$N_0 = \frac{10100N_2 - 10110V_1}{91} \Rightarrow Adm = \frac{10100 + 10110}{2 \times 91} \Rightarrow$$

Adm=111 V/V, Acm = 10100-10110 = - 1/9,1 V/V

CMRR=80 log 111/(1/9.1) = 60.1 dB.

[2.38] The imbalances are small enough to keep Adm = 1 V/V both in (a) and (b). Consequently, we only need to find the worst case value of Acm. Tie the rights together, apply VIC, and find Vac.

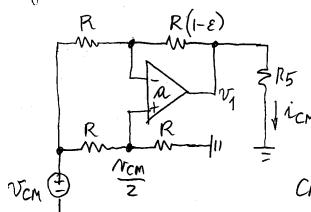


(a) Superposition:  $N_{OC} = -\frac{10}{10} V_{IC} - \frac{10}{10} V_{I}$ ,  $N_{I} = -\frac{10(1+\epsilon)}{10} N_{IC}$ :  $N_{OC} = -N_{I} + (1+\epsilon) V_{IC} = E N_{IC} \Rightarrow A_{CM} = E = 4 \frac{P}{100} = 4 \frac{0.1}{100} = \frac{1}{250} V_{N}$ .  $CMRR = 20 log 1/(1/250) \approx 48 dB$ 

(b) Only the even she to OA; matters, since that due to OA2 affects both inputs equally. OA1:  $\beta = 0.5$ ,  $T_i = 0.5 \times 10^4$ ,  $N_1 = -\frac{10}{10} \frac{1}{1+1/T_i}$   $N_{IC} = -1 \left(1 - \frac{1}{T_i}\right) N_{IC} = -N_{IC} + \frac{N_{IC}}{T_i}$ .  $N_{OC} = N_{IC} \left(-1 + 1 + \frac{1}{T_i}\right)$   $\Rightarrow A_{CM} = 1/T_i = 1/5000 \text{ V/V}$ .  $CMRR = 20\log 1/(1/5000) = 74 dB$ .

The imbalances of (a) and (b) are small arough to answer Adm 1/R5 in both cases. We therefore need only to find the worst case value of Acm. Tie the inputs together, apply VCM, and find icm. With a short-circuit load, OAz will return o V regardless of whether az = 00 or az = 103 V/V, so we can replace it

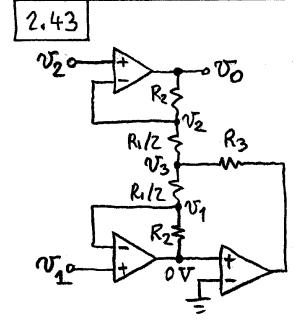
by a mere wine.



(a) A=00,  $E=4\frac{P}{100}=0.04$ . Superposition:  $V_1=-\frac{R(I-E)}{R}U_{CM}$   $+\left[1+\frac{R(I-E)}{R}\right] \frac{1}{2}V_{CM} = \frac{E}{2}V_{CM}$ ,  $I_{CM}=\frac{V_1}{R_5}=\frac{E/2}{R_5}$ . CMRR=20 log  $\frac{1/R_5}{(E/2)/R_5}=20\log 50=34dB$ .

(b) E=0, A=103 V/V. B=1, T=AB=500, VI=[-RVCM+(I+R)1 VCM] -1=0NCM-1+1/T=>Acm=0> CMRR=00. 2.40  $V_{N1} = V_{P1} = V_1 = 5V - 5$  sin wt mV;  $V_{N2} = V_{P2} = V_2 = 5V + 5$  sin wt mV;  $V_{O1} = V_{N1} + R_3 \frac{V_{N1} - V_{N2}}{R_G} = 5V - 5$  sin wt mV +  $\frac{10^6}{2\times10^3}(-10 \text{ sin at mV}) = 5V - 5.005$  sin wt V;  $V_{O2} = 5V + 5.005$  sin wt V;  $V_{N3} = V_{P3} = \frac{R^2}{R_1 + R_2} V_{O2} = 2.5V + 2.5025$  sin wt V;  $V_{O3} = \frac{R^2}{R_1} (V_{O2} - V_{O1}) = 10.01$  sin wt V.

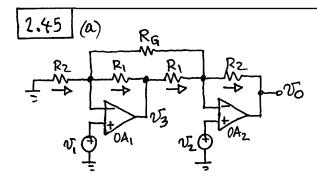
[2.42] From Problem 2.34,  $\beta_I = 1/A_I = 1/90$  V/V; moreover,  $\beta_{II} = 1/A_{II} = 1/20$  V/V. We can guarantee a 0.1% maximum deviation of  $A = A_I \times A_{II}$  from ideality by imposing a 0.05% maximum deviation of  $A_I$  and  $A_{II}$ . Thus,  $100/a_I\beta_I \leq 0.05 \Rightarrow a_I > 100 \times 50/0.05 = 10^5$  V/V; likewise,  $a_{II} > 4 \times 10^4$  V/V.



$$V_{1} = \frac{R_{2}}{R_{2} + R_{1}/2} V_{3} \Rightarrow V_{3} = \left(1 + \frac{R_{1}}{2R_{2}}\right) V_{1};$$

$$\frac{V_{0} - V_{2}}{R_{2}} = \frac{V_{2} - V_{3}}{R_{1}/2}.$$
Eliminating  $V_{3}$ ,
$$V_{0} = \left(1 + \frac{2R_{2}}{R_{1}}\right) \left(V_{2} - V_{1}\right).$$

2.44 (a) Superposition:  $V_0 = \left[1 + \frac{R_2}{R_1}\right] \left[V_{CM} + \frac{v_{DM}}{2}\right] - \frac{R_2}{R_1}\left[1 + \frac{R_1}{R_2}(1-\epsilon)\right] \left[V_{CM} - \frac{v_{DM}}{2}\right]$   $= \left(1 + \frac{R_2}{R_1} - \frac{\epsilon}{2}\right) v_{DM} + \epsilon v_{CM}$ (b) With 1% resistors,  $\epsilon$  can be as large as 0.04. Since this is much less than 100, we can write CMRR >  $20\log_{10}\left(100/0.04\right) = 68 \text{ dB}$ .



 $v_{M} = v_{p_1} = v_1$ ,  $v_{N2} = v_{p_2} = v_2$ . Applying KCL:  $\frac{O-v_1}{R_2} = \frac{v_1-v_2}{R_6} + \frac{v_1-v_3}{R_1}$ ;  $\frac{v_2-v_0}{R_2} = \frac{v_1-v_2}{R_6} + \frac{v_3-v_2}{R_1}$ . Adding the two equations pairwise gives  $\frac{v_2-v_1}{R_2} - \frac{v_0}{R_2} = 2\frac{v_1-v_2}{R_6} + \frac{v_1-v_2}{R_1}$ . Solving for  $v_0 = (1 + \frac{R_2}{R_1} + 2\frac{R_2}{R_6})(v_2-v_1)$ .

(b) Let  $R_G = R_{GA} + R_{GB}$ , where  $R_{GA} = 10$ -k.  $\Omega$  pot. Arbitrarily impose  $R_Z/R_1 = 1$ , so that  $A = 2(1 + R_Z/R_G)$ .  $10 \le A \le 100 \Rightarrow 5 \le (1 + R_Z/R_G) \le 50 \Rightarrow 4 \le R_Z/R_G \le 49$ .  $R_G = 0 + R_{GB} \Rightarrow R_Z/R_{GB} = 49$ ;  $R_G = 10 + R_{GB} \Rightarrow R_Z/(10 + R_{GB}) = 4$ . Solving,  $R_{GB} = 889 \Omega$  (use  $887\Omega$ , 1%);  $R_Z = 49R_{GB} = 43.5 k\Omega = R_1$  (use  $R_1 = R_2 = 43.2 k\Omega$ , 1%).

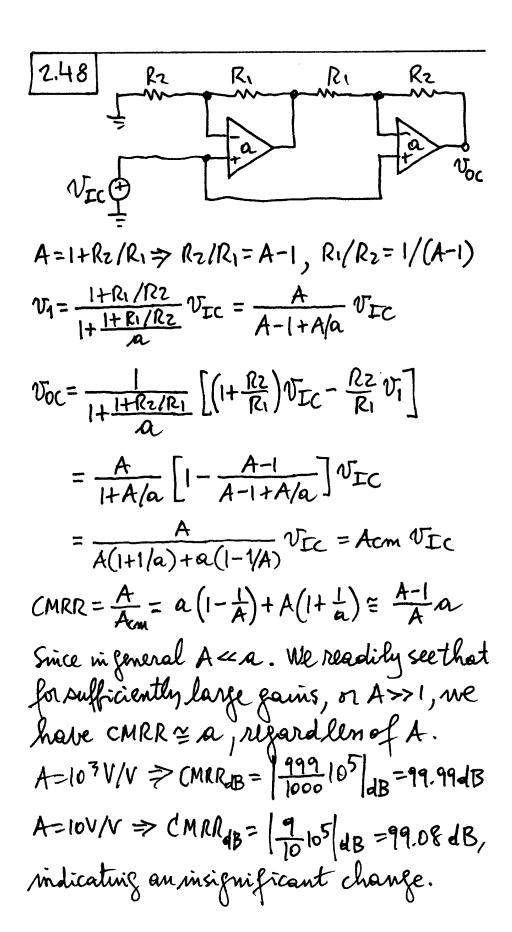
2.46 (a) The openings keep  $v_{P1} = v_{N1} = v_{1}$ ,  $v_{N2} = v_{P2} = v_{2}$ . Let  $v_{3}$  be the output of  $v_{N2}$ . Summing currents at  $v_{P1}$  and  $v_{N2}$  gives  $\frac{v_{0} - v_{2}}{R} + \frac{v_{1} - v_{2}}{R_{G}} + \frac{v_{3} - v_{2}}{R} = 0$   $\frac{v_{3} - v_{1}}{R} + \frac{v_{2} - v_{1}}{R_{G}} + \frac{v_{2} - v_{1}}{R} = 0$ Eliminating  $v_{3}$  and collecting gives  $v_{0} = 2\left(1 + \frac{R}{R_{G}}\right)\left(v_{2} - v_{1}\right) - v_{1}$ 

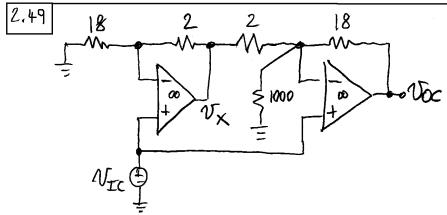
(b) Let RG be a 10-hr pot in serves with a resistance Rs. Then,

$$2\left(1+\frac{R}{R_s}\right)=100 \Rightarrow R=49R_s$$

Rs=888 I (mse 887 II, 1%), R=43.5 kI (use 43.2 kR, 1%).

[2.47] Regard the capacitor as an open circuit in dc analysis. By op amp action,  $\nabla_{P1} = \nabla_{N1} = \nabla_1$ ,  $\nabla_{N2} = \nabla_{P2} = \nabla_2$ . Moreover, the output of  $OA_2$  is  $V_3 = (1+R_1/R_2)\nabla_1 = -\frac{R_1}{R_2}\nabla_0 + (1+\frac{R_1}{R_2})\nabla_2$ . Thus,  $\nabla_0 = (1+\frac{R_2}{R_1})(\nabla_2 - \nabla_1)$ .



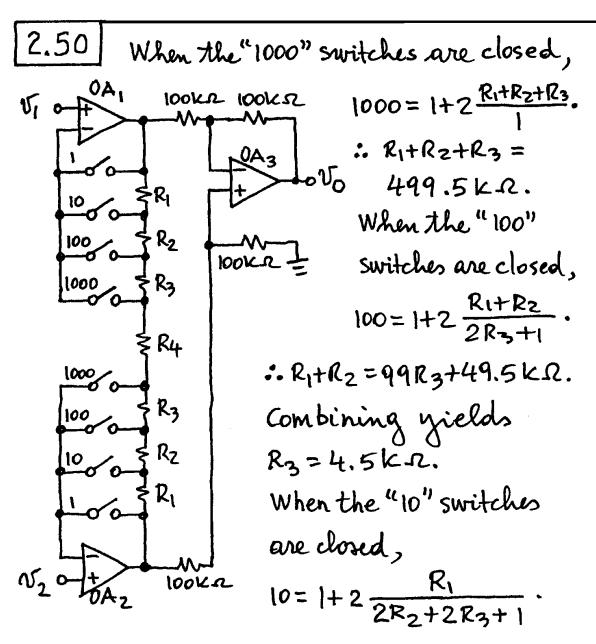


(a) Since IMSR > 18 kR > 2 kR, we expect the I-M  $\Omega$  resistor to have little effect on Adm, so  $Adm \approx 1+18/2=10$  V/V. To find Acm, the the inputs together and drive them with  $N_{TC}$ . Then, wring the superposition principle,  $N_{TC} = -\frac{18}{2}N_X + \left(1 + \frac{18}{2/1000}\right)N_{TC} = -9\left(1 + \frac{2}{18}\right)N_{TC} + \left(1 + \frac{18}{2} + \frac{18}{1000}\right)N_{TC}$ 

 $= \left(-10 + 10 + \frac{9}{500}\right) N_{TC} \Rightarrow A_{cm} = \frac{N_{OC}}{N_{TC}} = \frac{9}{500}.$ 

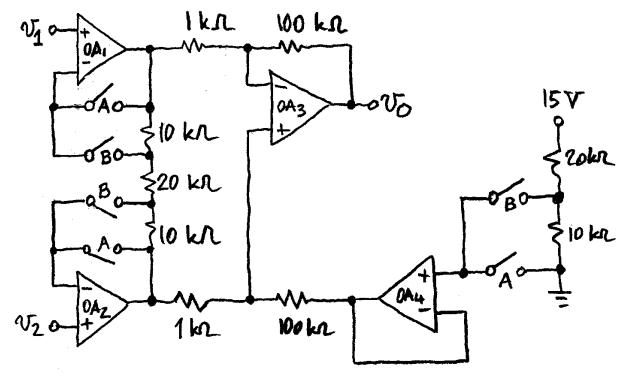
CMRR=20 log 10/(9/500) = 54.9 dB.

(b) NNZ = NPZ = NIC = i MNZ = 0, so the presence of the 1-MSI resistance has no effect on the CMRR in this case.



:.  $R_1 = 9R_2 + 45k\Omega$ . Combining yields  $R_2 = 45k\Omega$  and  $R_1 = 450k\Omega$ . Summarizing,  $R_1 = 450k\Omega$ ,  $R_2 = 45k\Omega$ ,  $R_3 = 4.5k\Omega$ ,  $R_4 = 1k\Omega$ . All other resistors = 100 k $\Omega$ .

## 2.51



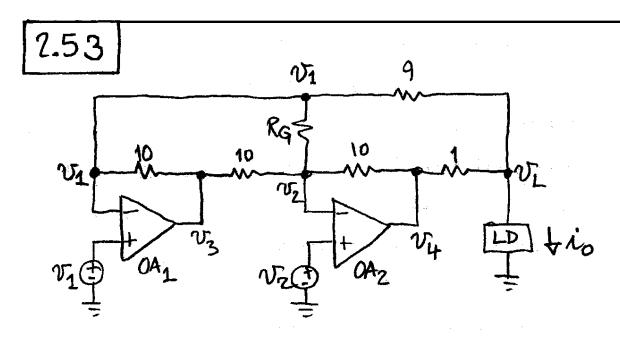
"A" switches closed  $\Rightarrow$   $V_0 = 1 \times 100 (V_2 - V_1) + 0 \text{ V}.$ "B" switches closed  $\Rightarrow$   $V_0 = (1 + 2\frac{10}{20}) \times 100 (V_2 - V_1) + 5 \text{ V}.$ 

2.52 (a) Let the aut puts of CA1 and Chr be Not and Noz. Superposition: Vo1 = (HKI)VI - KIVI V02= (1+ R5) V2 - Ru [(1+ R1) V1 - R1 VL] KCL: 10 =  $\frac{v_1-v_L}{R_2} + \frac{v_{02}-v_L}{R_2} \cdot Eliminating voz,$ is= \frac{\mathbb{V}\_2}{R\_2} \left[ 1 + \frac{R\_5}{R\_4} \right] - \frac{\mathbb{V}\_1}{R\_2} \left[ \frac{R\_5}{R\_4} \left( 1 + \frac{R\_1}{R\_2} \right) - \frac{R\_2}{R\_3} \right] - \mathbb{V}\_L \times Rz R3 Rz R3 . It is readily seen that imposing Rz+R3 = R.R5/R4 gives

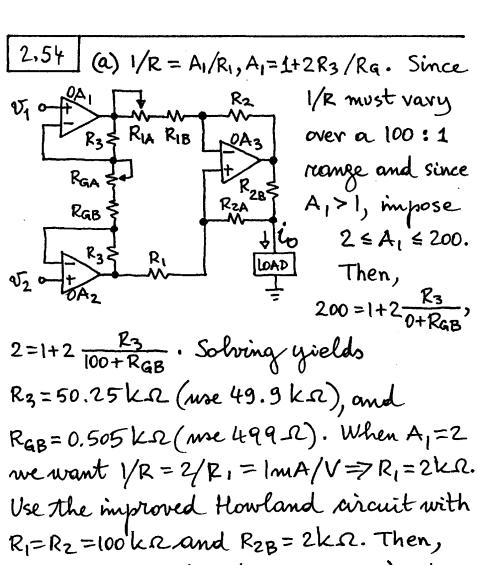
io= + (12-Vi), += HR5/R4.

(b) Use R1=R4=R5=100 KD, R2=2.00 KD, and R2 = 100-2= 98.0 kR.

(c) If the resistances are mismatched, the gains with which the aircuit processes of and vz will also be mismatched. Moreover, Ro \$00. Ro is minimized when R2, R3, and Ry are maximized, R, and R5 are minimized.  $R_0(min) = \frac{2 \times 10^3 \times 98 \times 10^3}{10^5 \times 1.001 - (10^5 \times 0.999)^2 / (10^5 \times 1.001)} = 490 \text{ kp.}$ 



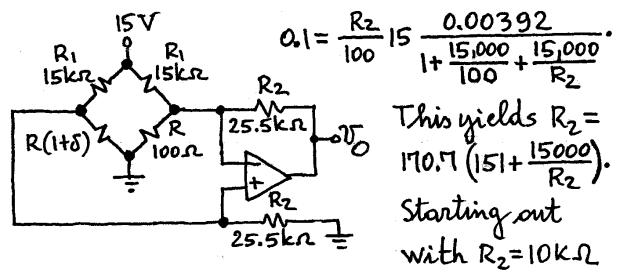
Summing currents at the inverting inputs of the  $\frac{V_L-V_I}{Q} + \frac{V_Z-V_I}{R_Q} + \frac{V_Z-V_I}{10} = 0$   $\frac{V_I-V_Z}{R_Q} + \frac{V_Z-V_Z}{10} + \frac{V_Z-V_Z}{10} = 0$ Solving for  $V_L$  gives  $V_L = \frac{10}{Q}V_L + V_Z\left(\frac{20}{R_Q} + 2\right) - V_L\left(\frac{20}{R_Q} + \frac{19}{9}\right) \cdot \text{kcl};$   $\dot{V}_0 = \frac{V_I-V_L}{Q} + \frac{V_L-V_L}{1}. \text{ Substituting } V_L \text{ fives}$   $\dot{V}_0 = 2\left(1 + \frac{10}{R_Q}\right)\left(V_Z-V_I\right).$ 



 $R_{12}R_{2}=100\,\text{k.C.}$  and  $R_{2}B=2\text{k.C.}$  (use 97.6k.R). Now 4% of 100 k.R. is 4k.R. Use  $R_{1A}=10\text{k.R}$  to be on the safe side, and  $R_{1}B=95.3$  k.R. Summarizing,  $R_{1}=R_{2}=100\text{k.R}$ ,  $R_{1}=R_{2}=100\text{k.R}$ ,  $R_{1}=R_{2}=100\text{k.R}$ ,  $R_{1}=R_{2}=100\text{k.R}$ ,  $R_{1}=R_{2}=100\text{k.R}$ ,  $R_{2}=100\text{k.R}$ ,  $R_{2}=100\text{k.R}$ ,  $R_{2}=100\text{k.R}$ ,  $R_{2}=100\text{k.R}$ ,  $R_{3}=100\text{k.R}$ ,  $R_{3}=100\text{k.R}$ ,  $R_{4}=100\text{k.R}$ ,  $R_{5}=100\text{k.R}$ ,  $R_{6}=100\text{k.R}$ ,  $R_{6}=1000\text{k.R}$ ,  $R_{6}=100\text{k.R}$ ,  $R_{6}=100\text{k.R}$ ,  $R_{6}=100\text{k.R}$ 

Ry as in Fig. 2.9.

2.55 With reference to Fig. 2.34, we want  $2R_2R_3/R_1 = 10 \text{ V/mA} = 10 \text{ k}\Omega$ . Let  $R_1 = R_2 = 10.0 \text{ k}\Omega$ . Then,  $R_3 = 10/2 = 5 \text{ k}\Omega$  (use 4.99 k/2, 1%). Moreower,  $R_4 = 4.99 \text{ k}\Omega$ , %.



and solving by iteration yields  $R_2 = 25.8 \text{ k.s.}$ 

(b) 
$$V_0 = \frac{25.5}{0.1} 15 \frac{0.392}{\frac{15}{0.1} + (1 + \frac{15}{25.5})(1 + 0.392)} =$$

9.96V, which corresponds to a 0.4°C error.

2.57 (a) KCL at the op amp input modes: VREF-VN = VN + VN-VO and VREF-VP = VP + VO R2. Letting VN = Vp and solving for Vo yields Vo = (R2/R)[S/(1+5)]Vp. Voltage divider:  $\frac{V_{P}}{V_{REF}} = \frac{[R(1+\delta)]/R_{2}}{[R(1+\delta)]/R_{2}+R_{1}} = \frac{1}{1+\frac{R_{1}}{[R(1+\delta)]/R_{2}}} = \frac{1}{[R(1+\delta)]/R_{2}}$  $\frac{1}{1+R_1\frac{R(1+S)+R_2}{R(1+S)R_2}} = \frac{1}{1+\frac{R_1}{R_2}\left(1+\frac{R_2}{R}\frac{1}{1+S}\right)}$  $\frac{1+\delta}{1+\delta(1+\frac{R_1}{R_2})+\frac{R_1}{D}} \cdot Eliminating Vp yields$ lim  $V_0 = \frac{R^2}{R} V_{REF} \frac{\delta}{1 + R \cdot 10 + R \cdot 10^2}$ (b) The output of OA1 is  $V_1 = -\frac{R(1+\delta')}{R_i}$ Superposition:  $v_0 = -(R_2/R)v_1 - (R_2/R_1)V_{REF}$ . Eliminating vy, vo = (R2/R1) VREF 8.

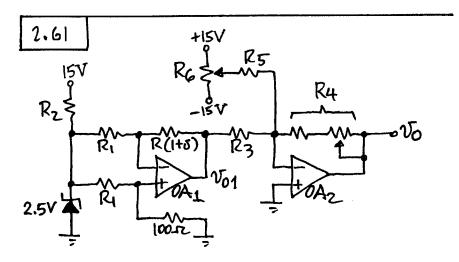
2.58 Impose Im A through each side of the bridge. Thus,  $R_1 = 2.5/2 = 1.25 \text{ kp. Let}$  R2=30 kp. and R = 100 p. both 1%. Then,  $0.1 = A \frac{100}{2 \times 1250} 2.5 \times 0.00392 \Rightarrow A = 255 \text{ V/V.}$ 

[2.59] (a) Let  $i_{RTD} = I_{mA}$ , so  $R_{1} = 15 \text{ kp.}$  Then,  $0.1 = \frac{R_{2}}{15,000} 15 \times 0.00392 \Rightarrow R_{2} = 25.5 \text{ kp.}$ (b) Use the same topology, components, and calibration procedure as in Example 2.13.

[2.60] Since  $v_N = v_P$ , it follows that the two legs of the bridge must conduct identical currents,

TREF-VO RI+R(1+8) = TREF RI+R. Thus, Vo=-RI+R VREFS.

The disadvantage is very low sensitivity, thus requiring an additional gain stage.



Let  $R_1=2.49 \text{ kp.}$ . Then,  $\Delta T=1^{\circ}C \Rightarrow \Delta v_{01}=$  [100/(100+2490)]×2.5×0.00392=378.38  $\mu V$ .  $\Delta v_{0}=(R_4/R_3)\Delta v_{01}=0.1 \text{ V} \Rightarrow R_4/R_3=264.3.$  Use  $R_3=1 \text{ kp.}$ ,  $R_4=237 \text{ kp.}$  in series with a 50-kp. pot. Let  $R_5=3.3 \text{ Mp.}$ ,  $R_6=100-\text{kp.}$  pot,  $R_2=3.9 \text{ kp.}$ . To calibrate: With  $T=0^{\circ}C$ , adjust  $R_6$  for  $v_0=0V$ . With  $T=100^{\circ}C$ , adjust  $R_4$  for  $v_0=10.0V$ .